



# Topology: Introduction

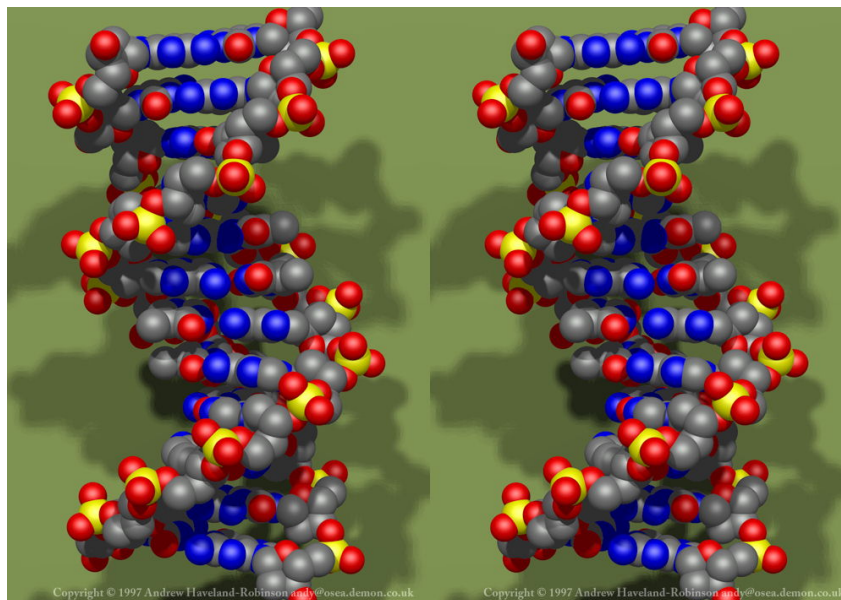
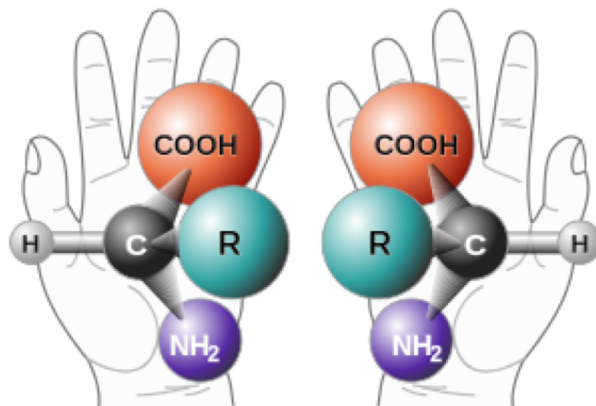


Claudia Felser



# Topology in Chemistry

Molecules with different chiralities can have different physical and chemical properties

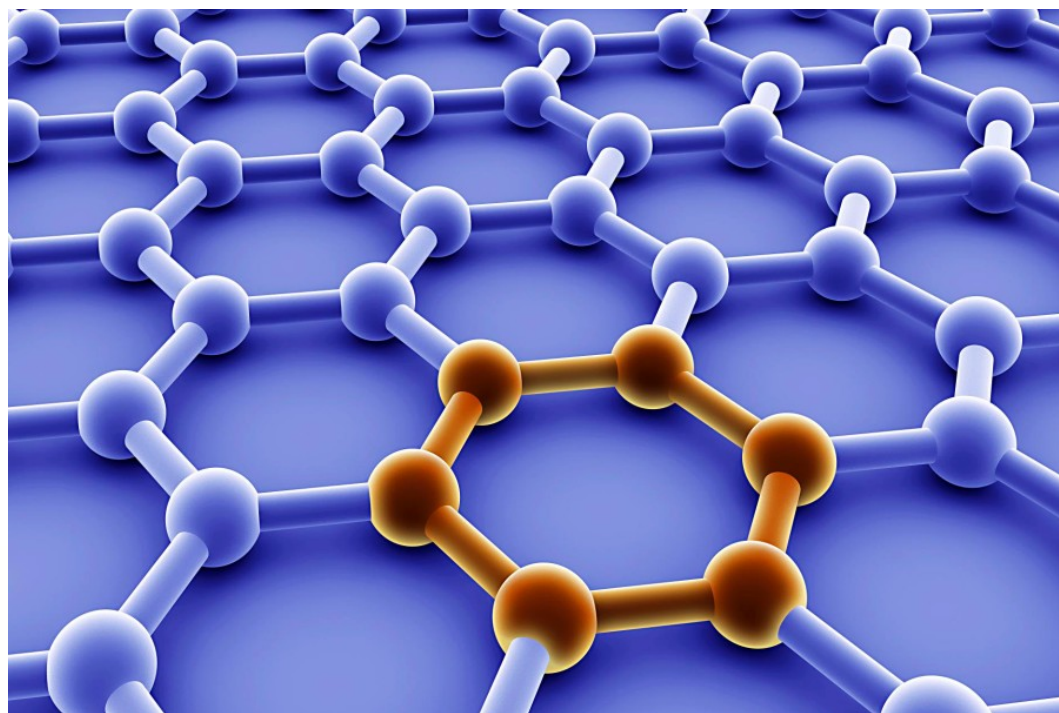
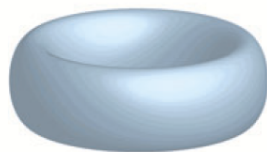
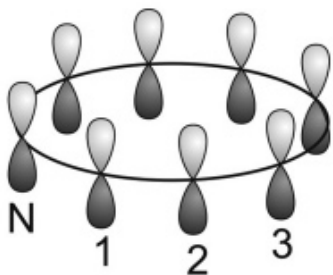
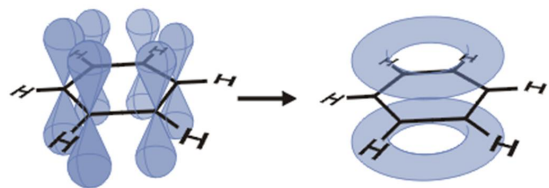
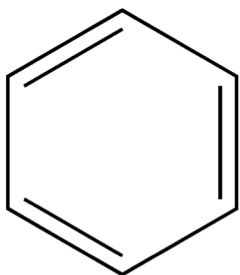




# Topology in Chemistry

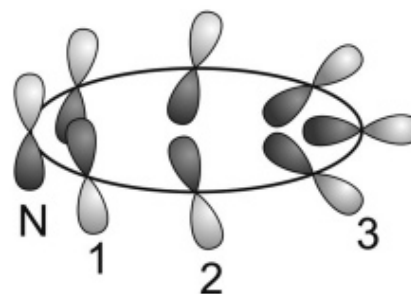
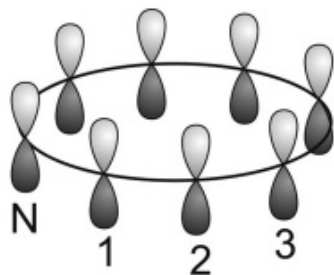
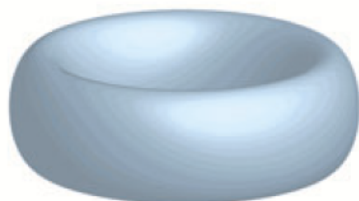
## Aromatic compounds

- Aromatic with  $(4n + 2) \pi$ -electrons
- The symmetry counts





# Topology in Chemistry



## Magic electron numbers

### Hückel:

$4n+2$  aromatic

$4n$  antiaromatic

### Möbius

$4n$  aromatic

$4n+2$  antiaromatic



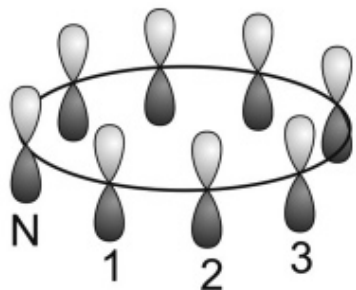
# Hückel and Möbius Aromaticity

## ORGANIC CHEMISTRY

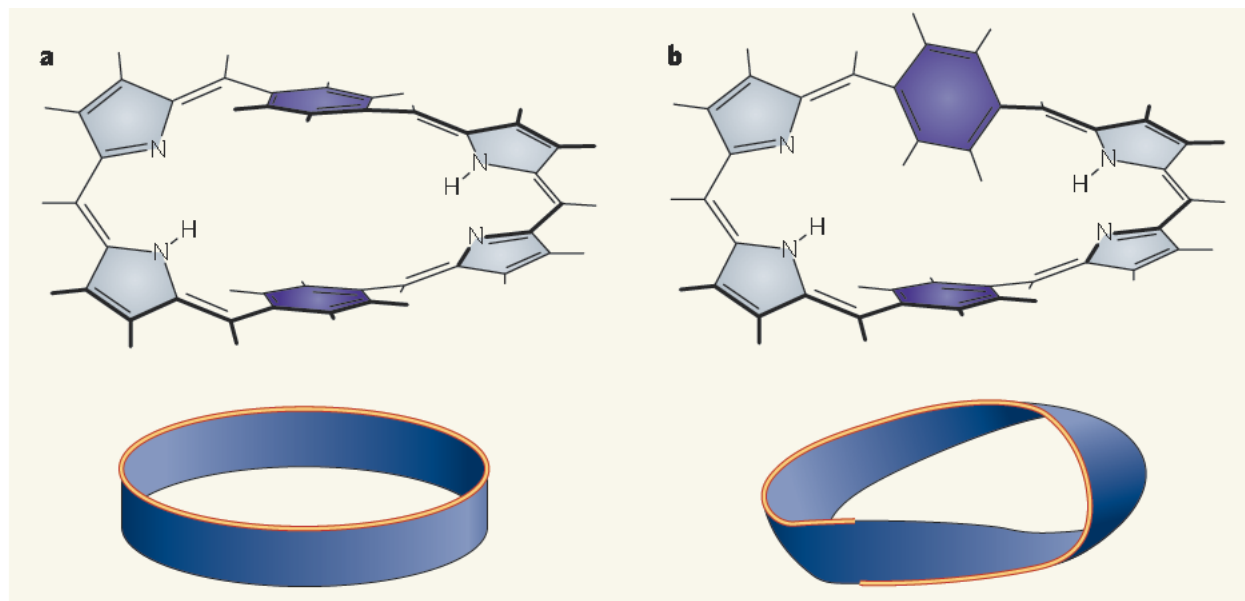
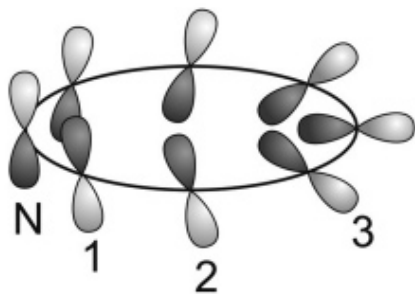
# Aromatics with a twist

Rainer Herges

The properties of flat aromatic molecules are well known to chemists, but some non-planar aromatics remain a mystery. A molecule that can twist into a Möbius band on command might shed light on their features.



Möbius Annulenes



**Figure 2 | A molecular topological switch.** Latos-Grażyński and colleagues<sup>1</sup> have made a compound that is antiaromatic in nonpolar solvents, but not in polar solvents. **a**, In nonpolar solvents, the two benzene rings (purple) in the molecule are parallel, and the molecule is a two-sided, non-twisted band. **b**, In polar solvents, the upper benzene ring twists by 90°, so that the molecule becomes a one-sided, Möbius structure. This conformational change alters the aromaticity of the molecule.



# The result

## Catalogue of Topological Electronic Materials

Tiantian Zhang,<sup>1,2,\*</sup> Yi Jiang,<sup>2,1,\*</sup> Zhida Song,<sup>1,2,\*</sup> He Huang,<sup>3</sup>  
Yuqing He,<sup>3,2</sup> Zhong Fang,<sup>1</sup> Hongming Weng,<sup>1,†</sup> and Chen Fang<sup>1,4,‡</sup>

<sup>1</sup>*Beijing National Laboratory for Condensed Matter Physics,  
and Institute of Physics, Chinese Academy of Sciences, Beijing 100190, China*

<sup>2</sup>*University of Chinese Academy of Sciences, Beijing 100049, China*

<sup>3</sup>*Computer Network Information Center, Chinese Academy of Sciences, China*

<sup>4</sup>*CAS Centre for Excellence in Topological Quantum Computation, Beijing, China*

Preprints 1807.08756, 1807.10271

## The (“High-Quality”) Topological Materials In The World

M. G. Vergniory<sup>1,2,3\*</sup>

<sup>1</sup>*Donostia International Physics Center, P. Manuel de Lardizabal 4, 20018 Donostia-San Sebastián, Spain*

<sup>2</sup>*IKERBASQUE, Basque Foundation for Science,  
Maria Diaz de Haro 3, 48013 Bilbao, Spain and*

<sup>3</sup>*Applied Physics Department II, University of the Basque Country UPV/EHU, Apartado 644, 48080 Bilbao, Spain*

L. Elcoro<sup>1\*</sup>

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<sup>2</sup>*Physics Department, Freie Universität Berlin, Arnimallee 14, 14195 Berlin, Germany and*

<sup>3</sup>*Max Planck Institute of Microstructure Physics, 06120 Halle, Germany*

Zhijun Wang<sup>1‡</sup>

<sup>1</sup>*Department of Physics, Princeton University, Princeton, New Jersey 08544, USA*

(Dated: July 26, 2018)



# Bilbao crystallographics server



FCT/ZTF

## bilbao crystallographic server



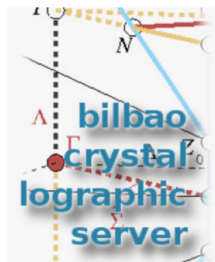
UPV EHU

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### ECM31-Oviedo Satellite

Crystallography online:  
workshop on the use and  
applications of the  
structural tools of the  
Bilbao Crystallographic  
Server

20-21 August 2018

### News:

- **New program:**  
**mCIF2PCR**

01/2018: Transformation from  
mCIF to PCR format. The

Space-group symmetry
Magnetic Symmetry and Applications
Group-Subgroup Relations of Space Groups
Representations and Applications
Solid State Theory Applications
Structure Utilities
Subperiodic Groups: Layer, Rod and Frieze Groups
Structure Databases

**Quick  
access to  
some tables**

Space  
Groups

Plane  
Groups

Layer  
Groups

Rod Groups

Frieze  
Groups

2D Point  
Groups

3D Point  
Groups



Exactly Match Elements ↕

Cu & N



Search

1																	2
H																	He
3	4											5	6	7	8	9	10
Li	Be											B	C	N	O	F	Ne
11	12											13	14	15	16	17	18
Na	Mg											Al	Si	P	S	Cl	Ar
19	20	21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36
K	Ca	Sc	Ti	V	Cr	Mn	Fe	Co	Ni	Cu	Zn	Ga	Ge	As	Se	Br	Kr
37	38	39	40	41	42	43	44	45	46	47	48	49	50	51	52	53	54
Rb	Sr	Y	Zr	Nb	Mo	Tc	Ru	Rh	Pd	Ag	Cd	In	Sn	Sb	Te	I	Xe
55	56	57-71	72	73	74	75	76	77	78	79	80	81	82	83	84	85	86
Cs	Ba	La-Lu	Hf	Ta	W	Re	Os	Ir	Pt	Au	Hg	Tl	Pb	Bi	Po	At	Rn
87	88	89-103	104	105	106	107	108	109	110	111	112						
Fr	Ra	Ac-Lr	Rf	Db	Sg	Bh	Hs	Mt	Ds	Rg	Cn						

57	58	59	60	61	62	63	64	65	66	67	68	69	70	71
La	Ce	Pr	Nd	Pm	Sm	Eu	Gd	Tb	Dy	Ho	Er	Tm	Yb	Lu
89	90	91	92	93	94	95	96	97	98	99	100	101	102	103
Ac	Th	Pa	U	Np	Pu	Am	Cm	Bk	Cf	Es	Fm	Md	No	Lr



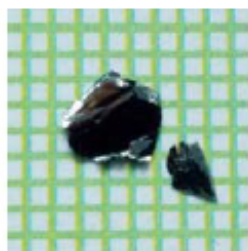


# Novel topological materials

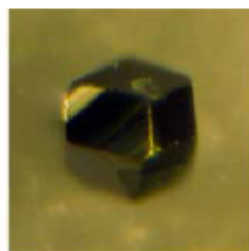
- Explorative search for new materials & predictive design (Yan Sun)
- **200** high quality **single crystal growth** (Shekhar Chandra)
- **Epitaxial growth** of thin films (Anastasios Markou)
- **2D materials – Nanowires** (Johannes Gooth)



Ag<sub>2</sub>Se 1000 μm



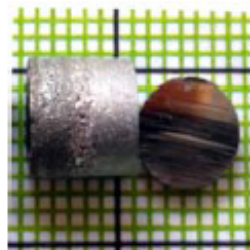
BiTeBr 3000 μm



CaPd<sub>3</sub>O<sub>4</sub> 100 μm



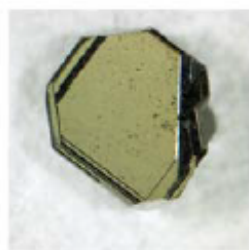
HfTe<sub>3</sub> 1000 μm



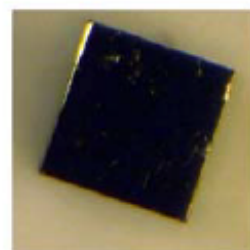
Mn<sub>3</sub>Ir 3000 μm



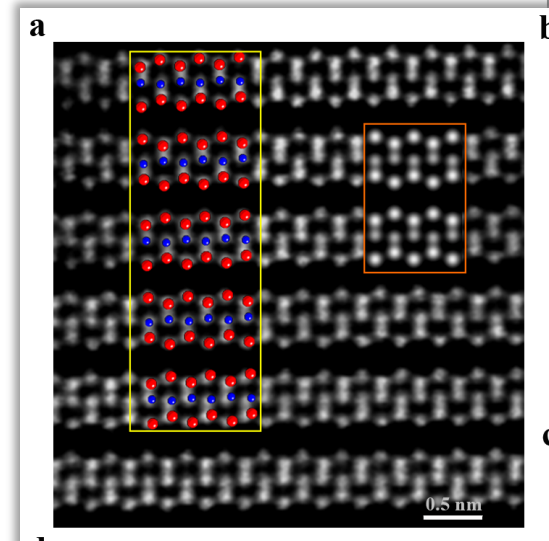
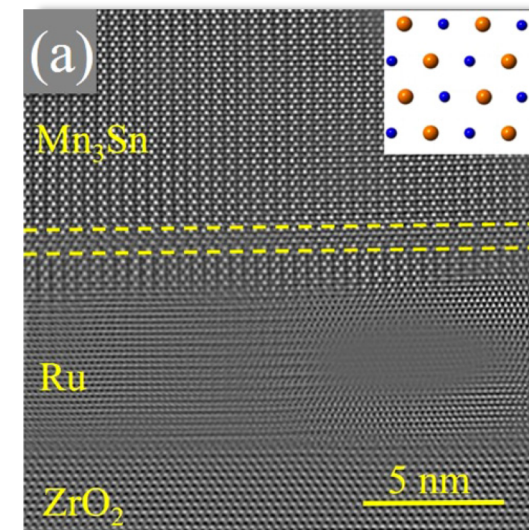
NbAs 2000 μm



NbP 2000 μm



SrPd<sub>3</sub>O<sub>4</sub> 100 μm



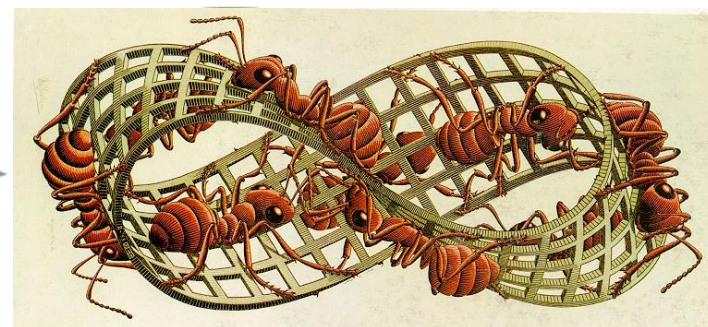
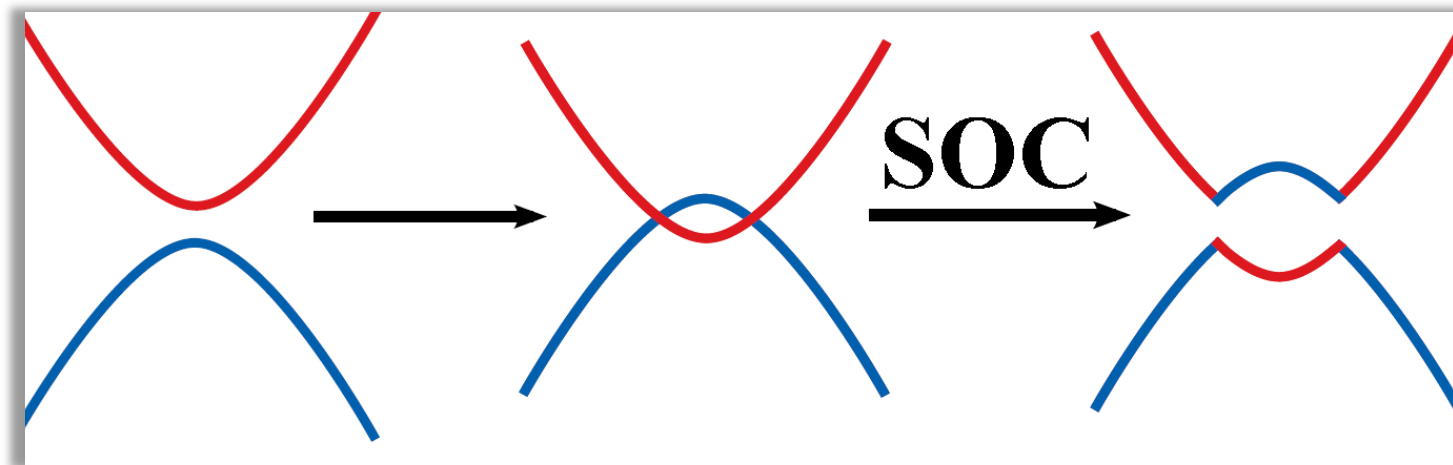


# Trivial and Topological Insulators

Trivial semiconductor  
CdS

Topological Insulator  
Without spin orbit coupling

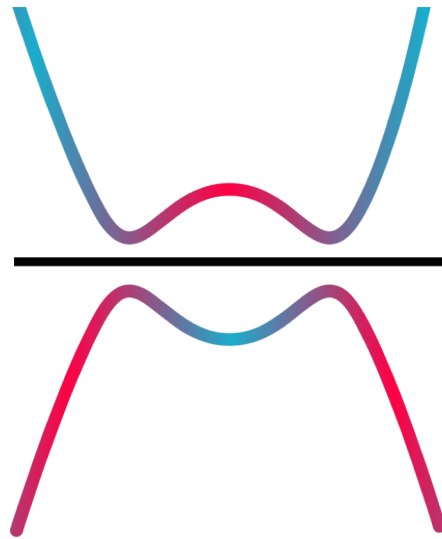
Topological Insulator  
With spin orbit coupling



M. C. Escher



# Topological Insulators





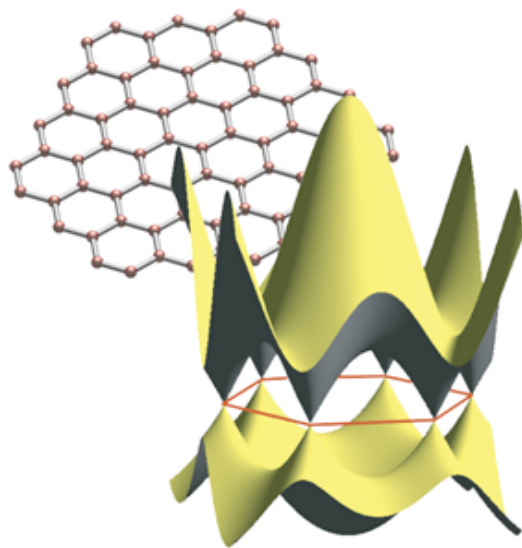
# Topological Insulators

## Z<sub>2</sub> Topological Order and the Quantum Spin Hall Effect

C.L. Kane and E. J. Mele

Department of Physics and Astronomy, University of Pennsylvania, Philadelphia, Pennsylvania 19104, USA  
(Received 22 June 2005; published 28 September 2005)

The quantum spin Hall (QSH) phase is a time reversal invariant electronic state with a bulk electronic band gap that supports the transport of charge and spin in gapless edge states. We show that this phase is associated with a novel Z<sub>2</sub> topological invariant, which distinguishes it from an ordinary insulator. The Z<sub>2</sub> classification, which is defined for time reversal invariant Hamiltonians, is analogous to the Chern number classification of the quantum Hall effect. We establish the Z<sub>2</sub> order of the QSH phase in the two band model of graphene and propose a generalization of the formalism applicable to multiband and interacting systems.



First prediction in graphene by Kane

Heavy insulating elements?

Strained  $\alpha$ -Sn and Bi-bilayer

H 2.20																	He	
Li 0.98	Be 1.57											B 2.04	C 2.55	N 3.04	O 3.44	F 3.98	Ne	
Na 0.93	Mg 1.31											Al 1.61	Si 1.90	P 2.19	S 2.58	Cl 3.16	Ar	
K 0.82	Ca 1.00	Sc 1.36	Ti 1.54	V 1.63	Cr 1.66	Mn 1.55	Fe 1.83	Co 1.88	Ni 1.91	Cu 1.90	Zn 1.65	Ga 1.81	Ge 2.01	As 2.18	Se 2.55	Br 2.96	Kr 3.00	
Rb 0.82	Sr 0.95	Y 1.22	Zr 1.33	Nb 1.60	Mo 2.16	Tc 1.90	Ru 2.20	Rh 2.28	Pd 2.20	Ag 1.93	Cd 1.69	In 1.78	Sn 1.96	Sb 2.05	Te 2.10	I 2.66	Xe 2.60	
Cs 0.79	Ba 0.89			Hf 1.30	Ta 1.50	W 1.70	Re 1.90	Os 2.20	Ir 2.20	Pt 2.20	Au 2.40	Hg 1.90	Tl 1.80	Pb 1.80	Bi 1.90	Po 2.00	At 2.20	Rn
Fr 0.70	Ra 0.90																	
		La 1.10	Ce 1.12	Pr 1.13	Nd 1.14	Pm 1.13	Sm 1.17	Eu 1.20	Gd 1.20	Tb 1.10	Dy 1.22	Ho 1.23	Er 1.24	Tm 1.25	Yb 1.10	Lu 1.27		
		Ac 1.10	Th 1.30	Pa 1.50	U 1.70	Np 1.30	Pu 1.28	Am 1.13	Cm 1.28	Bk 1.30	Cf 1.30	Es 1.30	Fm 1.30	Md 1.30	No 1.30	Lr 1.30		

$$\lambda_{\text{SOC}} \sim Z^2 \text{ for valence shells}$$



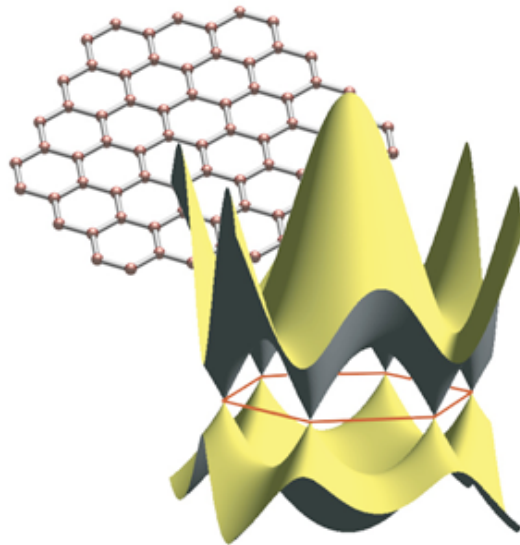
# Topological Insulators

## Z<sub>2</sub> Topological Order and the Quantum Spin Hall Effect

C. L. Kane and E. J. Mele

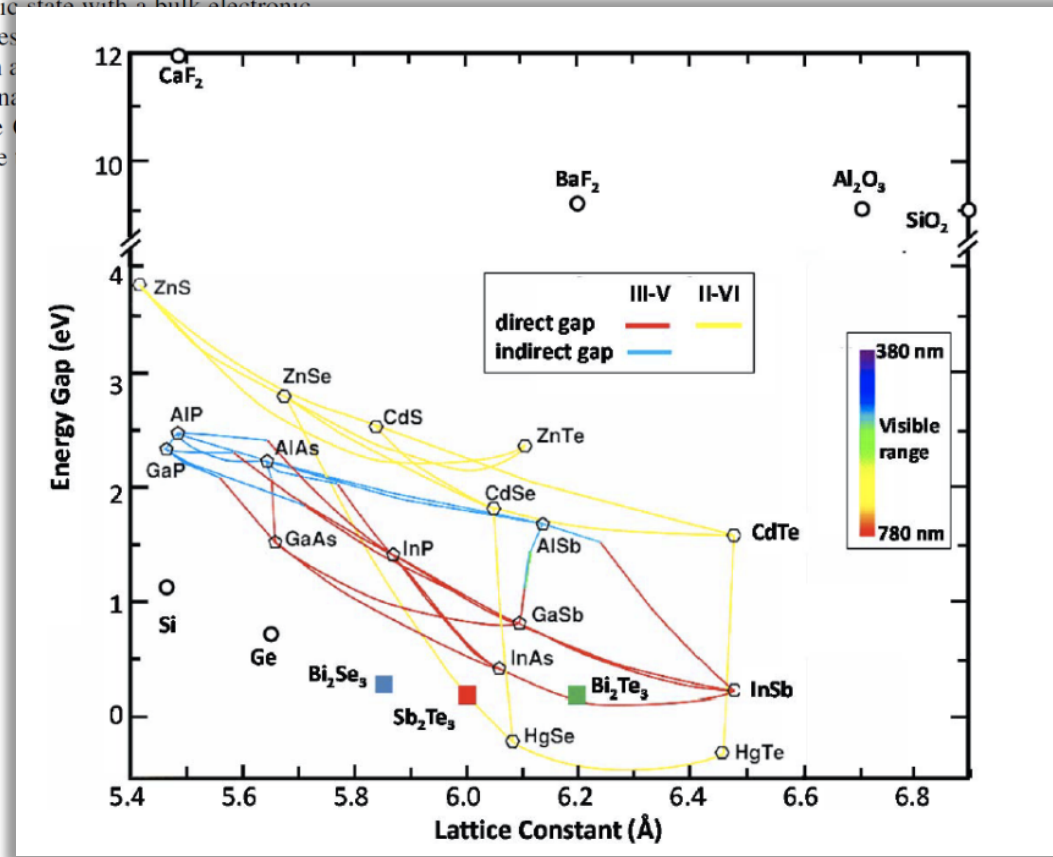
Department of Physics and Astronomy, University of Pennsylvania, Philadelphia, Pennsylvania 19104, USA  
(Received 22 June 2005; published 28 September 2005)

The quantum spin Hall (QSH) phase is a time reversal invariant electronic state with a bulk electronic band gap that supports the transport of charge and spin in gapless edge states associated with a novel Z<sub>2</sub> topological invariant, which distinguishes it from a classification, which is defined for time reversal invariant Hamiltonians, is another classification of the quantum Hall effect. We establish the Z<sub>2</sub> order of the model of graphene and propose a generalization of the formalism applicable to systems.



First prediction in graphene by Kane

## Heavy insulating binaries



Kane and Mele, PRL 95, 146802 (2005)  
 Bernevig, et al., Science 314, 1757 (2006)  
 Bernevig, S.C. Zhang, PRL 96, 106802 (2006)  
 König, et al. Science 318, 766 (2007)

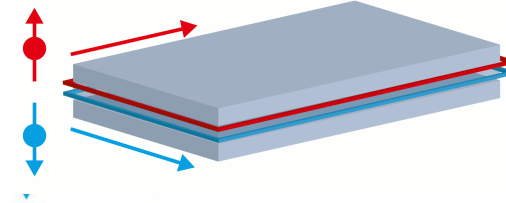
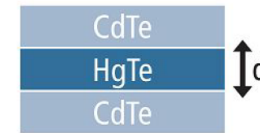
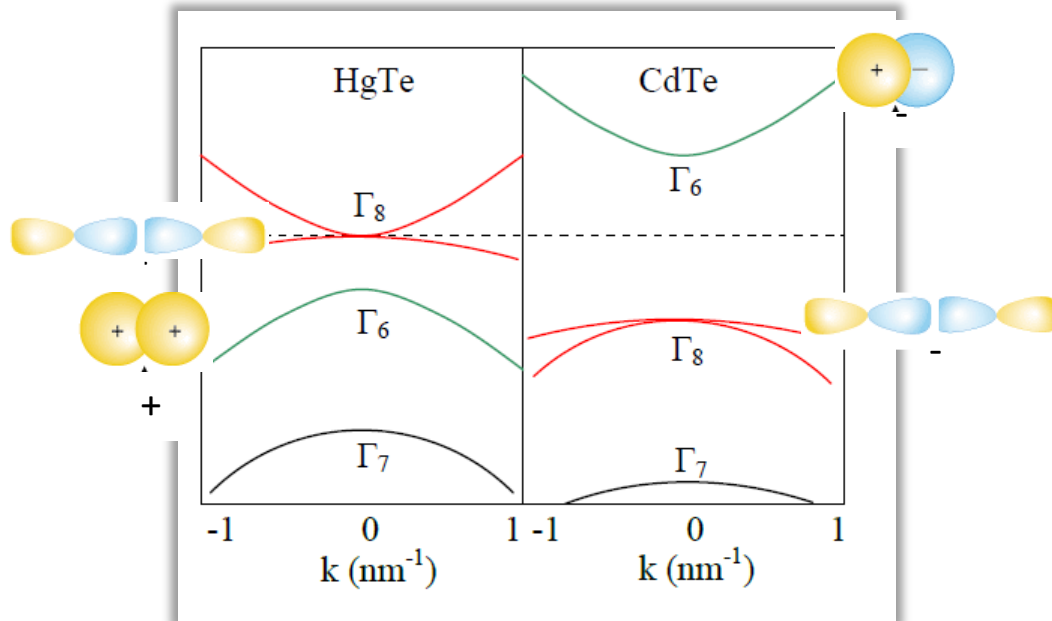


# Quantum Spin Hall



## Quantum Spin Hall Effect and Topological Phase Transition in HgTe Quantum Wells

B. Andrei Bernevig, et al.  
*Science* **314**, 1757 (2006);  
DOI: 10.1126/science.1133734



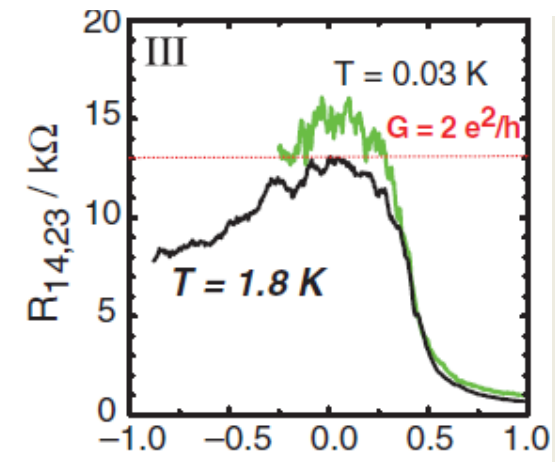
3D: Dirac cone on the surface  
2D: Dirac cone in quantum well

### Inert pair effect

Bernevig, et al., *Science* 314, 1757 (2006)

Bernevig, S.C. Zhang, *PRL* 96, 106802 (2006)

König, et al. *Science* 318, 766 (2007)



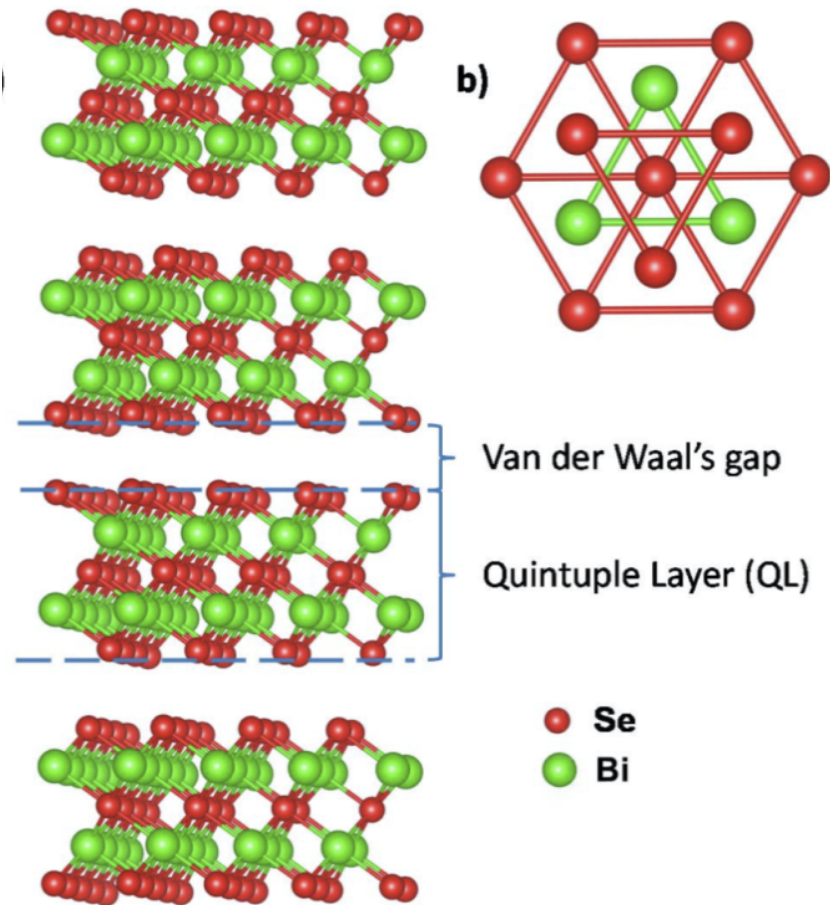
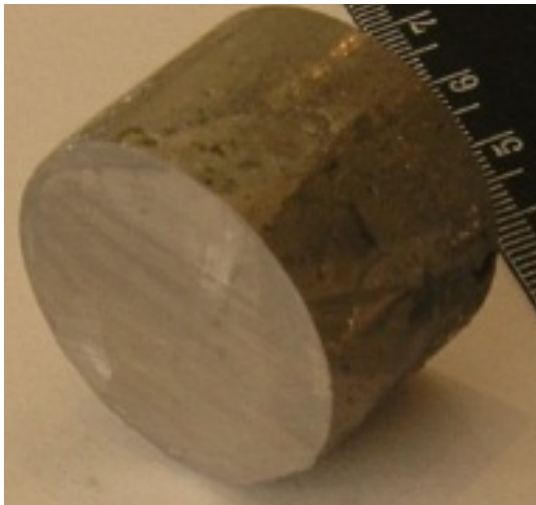


# Topologische Isolatoren

Starting with Bismuth

Bi-Sb Legierungen

$\text{Bi}_2\text{Se}_3$  und verwandte Strukturen



Moore and Balents, PRB 75, 121306(R) (2007)

Fu and Kane, PRB 76, 045302 (2007)

Murakami, New J. Phys. 9, 356 (2007)

Hsieh, et al., Science 323, 919 (2009)

Xia, et al., Nature Phys. 5, 398 (2009); Zhang, et al., Nature Phys. 5, 438 (2009)

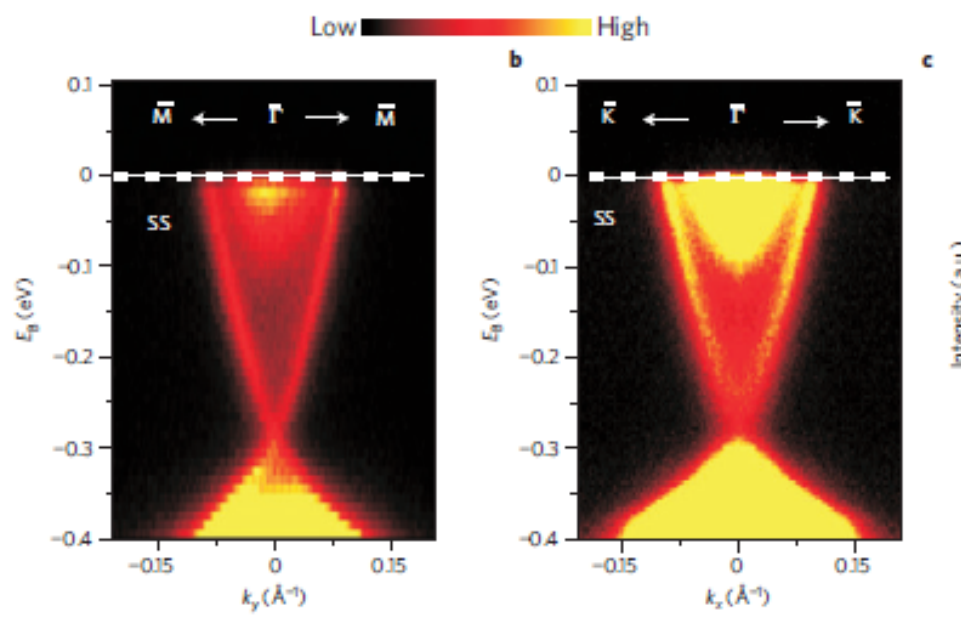
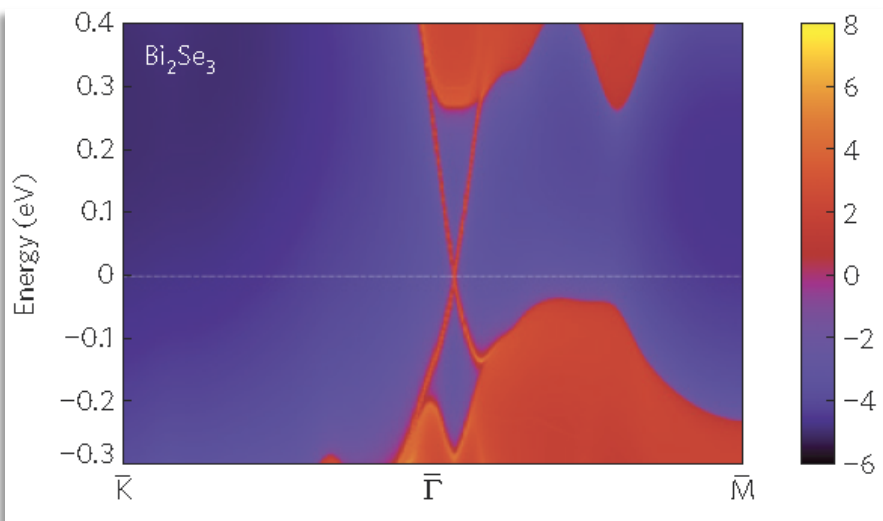
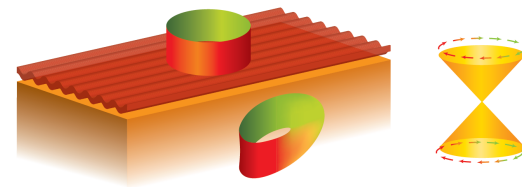


# Theory and experiment

## 3D topological insulators

Bi-Sb alloy

$\text{Bi}_2\text{Se}_3$  and relatives



Moore and Balents, PRB 75, 121306(R) (2007)

Fu and Kane, PRB 76, 045302 (2007)

Murakami, New J. Phys. 9, 356 (2007)

Hsieh, et al., Science 323, 919 (2009)

Xia, et al., Nature Phys. 5, 398 (2009); Zhang, et al., Nature Phys. 5, 438 (2009)

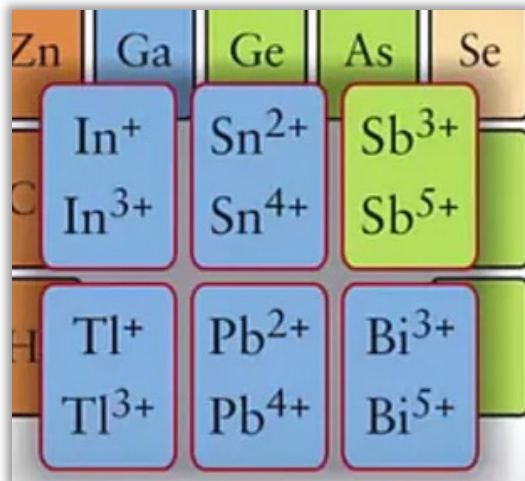




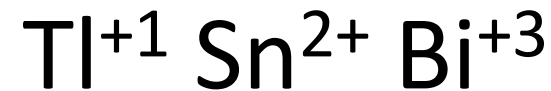
# Materials

Table I. Proposed topological insulator materials grouped into several different material classes.<sup>4,12,13,19,23-29</sup>

HgTe-type	Bi <sub>2</sub> Se <sub>3</sub> -type	Honey Comb Lattice	Bismuth-Alloys	NaCl Structure	Oxides	Correlated Materials	Super-conductors
HgTe	Bi <sub>2</sub> Se <sub>3</sub> , Bi <sub>2</sub> Te <sub>3</sub> , and Sb <sub>2</sub> Te <sub>3</sub>	Graphene	Bi-Sb	SnTe PbTe	Doped BaBiO <sub>3</sub>	Iridates	Cu <sub>x</sub> Bi <sub>2</sub> Se <sub>3</sub>
Half-Heuslers such as LaPtBi	Bi <sub>2</sub> Te <sub>2</sub> Se	LiAuTe		PuTe AmN	Iridates	SmB <sub>6</sub>	LaPtBi YPtBi LuPtBi
$\alpha$ -Sn, HgSe $\beta$ -HgS	(Bi <sub>x</sub> Sb <sub>1-x</sub> ) <sub>2</sub> Te <sub>3</sub>					YbPtBi	TlBiSe <sub>2</sub> TlBiTe <sub>2</sub>
Chalco-pyrites	TlBiSe <sub>2</sub> and TlBiTe <sub>2</sub>					Skutterudites	
AlSb/InAs/GaSb	Bi <sub>14</sub> Rh <sub>3</sub> I <sub>9</sub>					PuTe, AmN	



Claudia Felser and Xiao-Liang Qi , Guest Editors, MRS Bull. 39 (2014) 843.

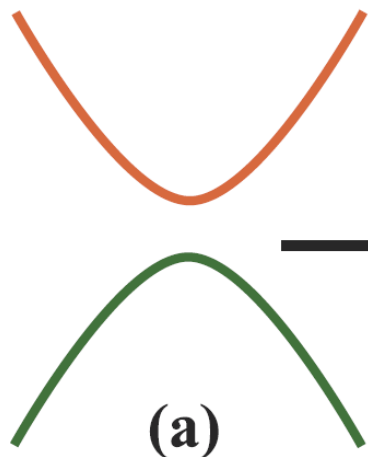


**Inert pair effect**

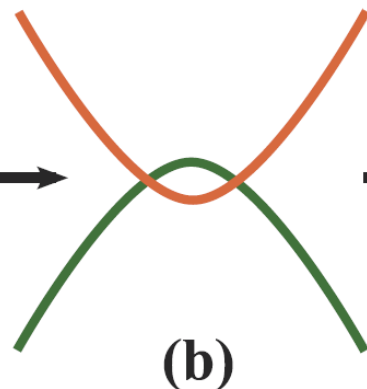


# Trivial and topological insulators

Trivial semiconductor  
CdS

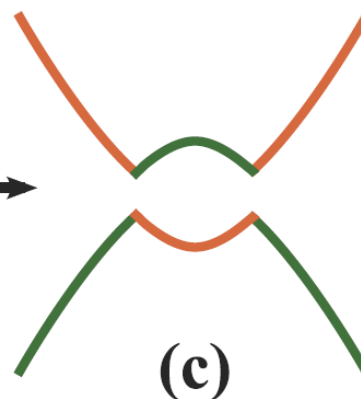


Topological Insulator  
Without spin orbit coupling



SOC

Topological Insulator  
With spin orbit coupling



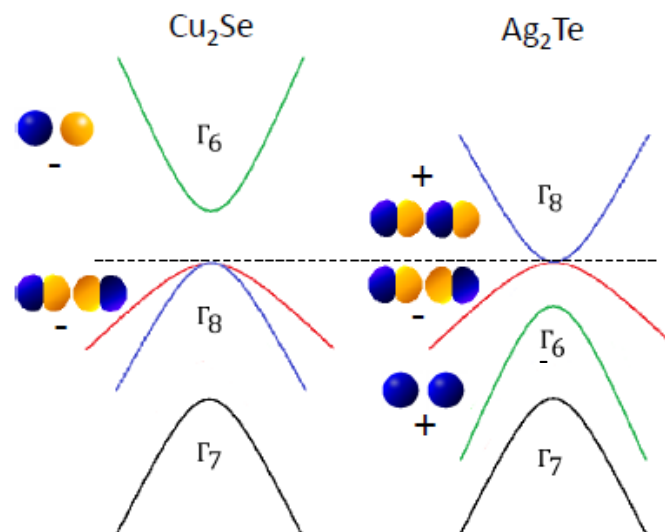
Sufficient condition:

Parity change

**Centro symmetric**  $\rightarrow$  **Eigenvalues**

Noncentro sym.  $\rightarrow$  **Z2 classification**

**Inert pair effect**

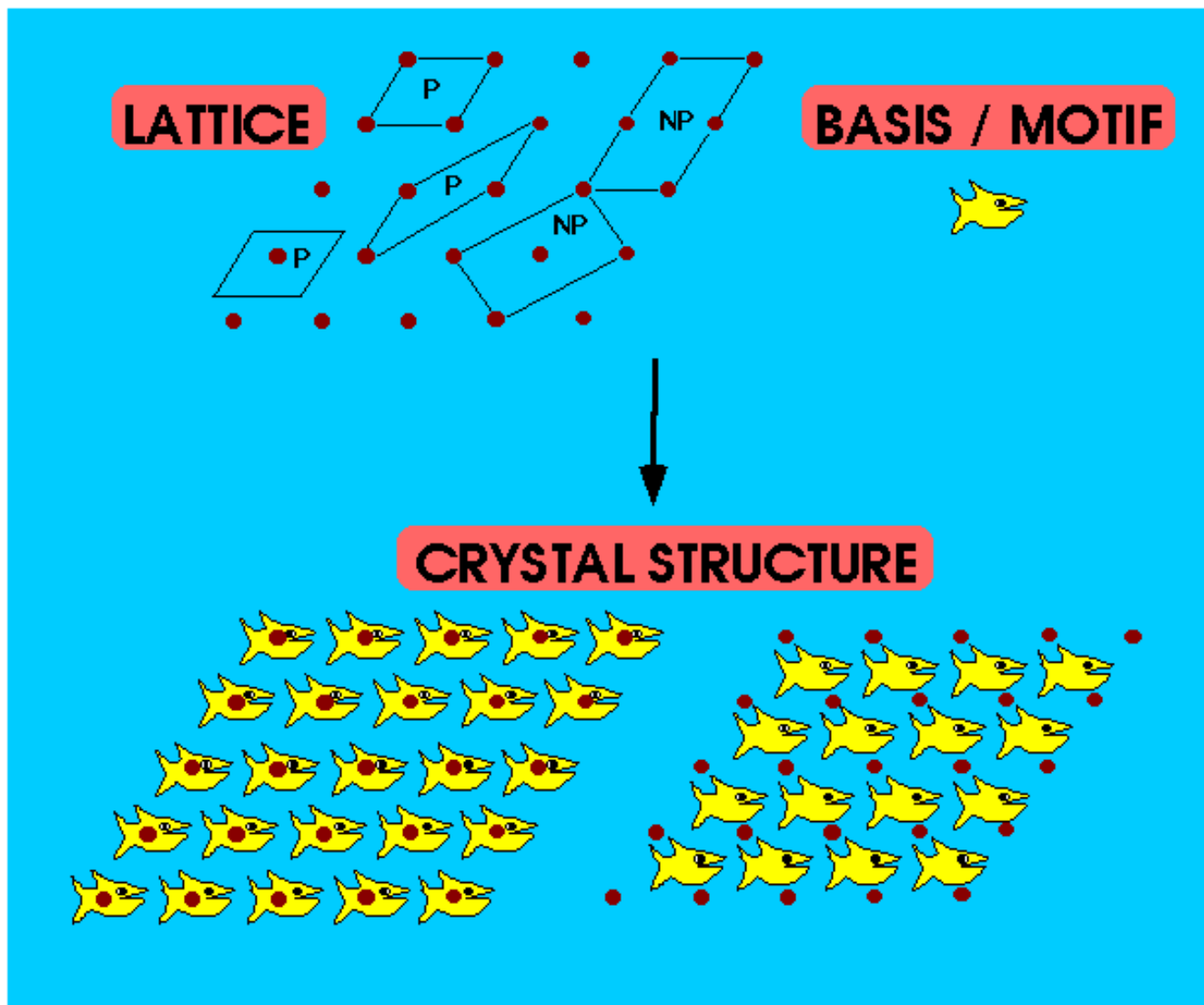




# Crystal structure



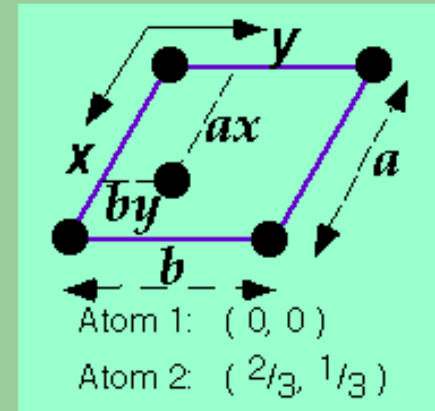
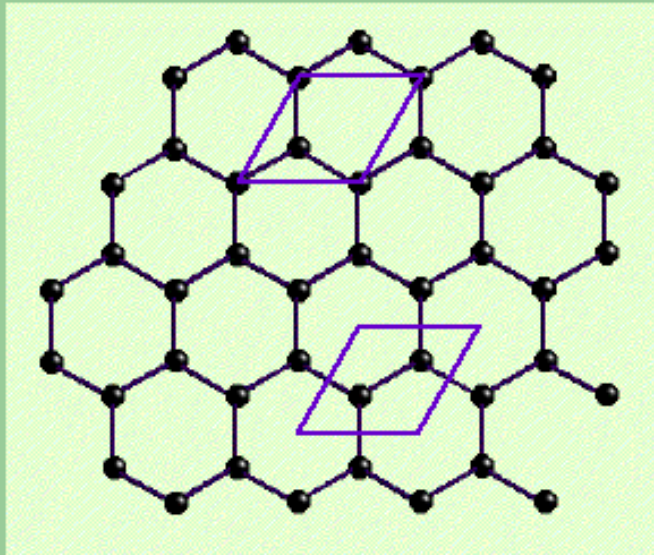
# Definitions



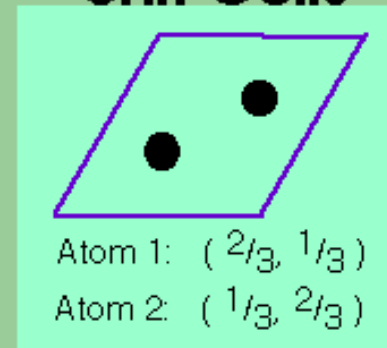


# Graphene

## 2D LATTICE



## Unit Cells



*FRACTIONAL Atomic  $(x,y)$  coordinates*  
(As a fraction of unit cell dimension)  
*i.e.* true dimensions are  $ax$  and  $by$

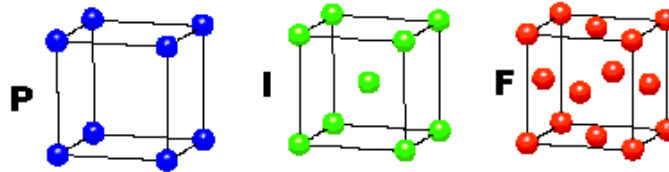


# Space groups

## CUBIC

$$a = b = c$$

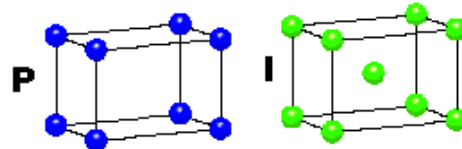
$$\alpha = \beta = \gamma = 90^\circ$$



## TETRAGONAL

$$a = b \neq c$$

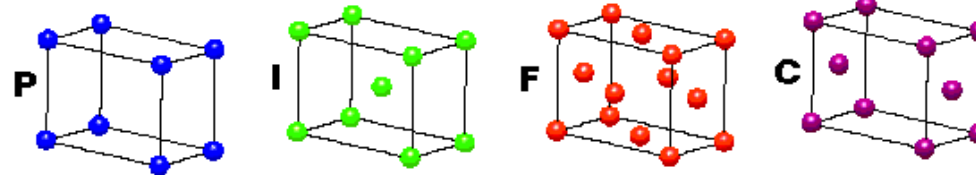
$$\alpha = \beta = \gamma = 90^\circ$$



## ORTHORHOMBIC

$$a \neq b \neq c$$

$$\alpha = \beta = \gamma = 90^\circ$$

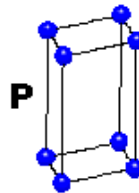


## HEXAGONAL

$$a = b \neq c$$

$$\alpha = \beta = 90^\circ$$

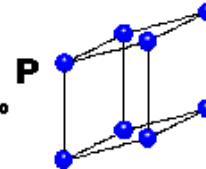
$$\gamma = 120^\circ$$



## TRIGONAL

$$a = b = c$$

$$\alpha = \beta = \gamma \neq 90^\circ$$

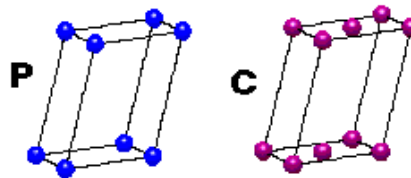


## MONOCLINIC

$$a \neq b \neq c$$

$$\alpha = \gamma = 90^\circ$$

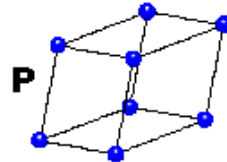
$$\beta \neq 120^\circ$$



## TRICLINIC

$$a \neq b \neq c$$

$$\alpha \neq \beta \neq \gamma \neq 90^\circ$$



### 4 Types of Unit Cell

P = Primitive

I = Body-Centred

F = Face-Centred

C = Side-Centred

+

7 Crystal Classes

→ 14 Bravais Lattices

230 space groups



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## ICSD - Inorganic Crystal Structure Database

FIZ Karlsruhe provides the scientific and the industrial community with the world's largest database for completely identified inorganic crystal structures, ICSD. The ICSD data are of excellent quality and its first records date back to 1913. Only data which have passed thorough quality checks are included.

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As the world's leading provider of scientific information on inorganic crystal structures, we take full responsibility for database production, maintenance and quality control, and we ensure that the ICSD database and our software solutions meet the highest possible quality standards.

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### Highlights:

- All important crystal structure data are available, including unit cell, space group, complete atomic parameters, site occupation factors, Wyckoff sequence, molecular formula and weight, ANX formula, mineral group, etc.
- 80 % of the structures are allocated to about 9,000 structure types. This allows for searches for substance classes.
- Continuous selection and evaluation of theoretical structures. They can serve as a basis for developing new materials through data mining processes.
- Keywords to describe to physical and chemical properties are provided.
- Abstracts for a quick grasp of the article content are available.
- Simulation of Powder Diffraction Data

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[Read more](#)



- Closed packed structures
  - Cubic
  - Hexagonal

The anion (neg. charged atom and therefore big) builds the closed packed structure

The cation is found in the voids

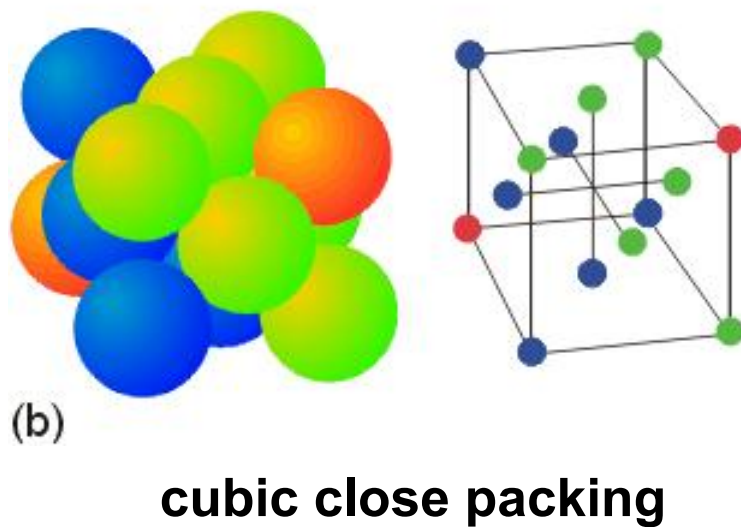
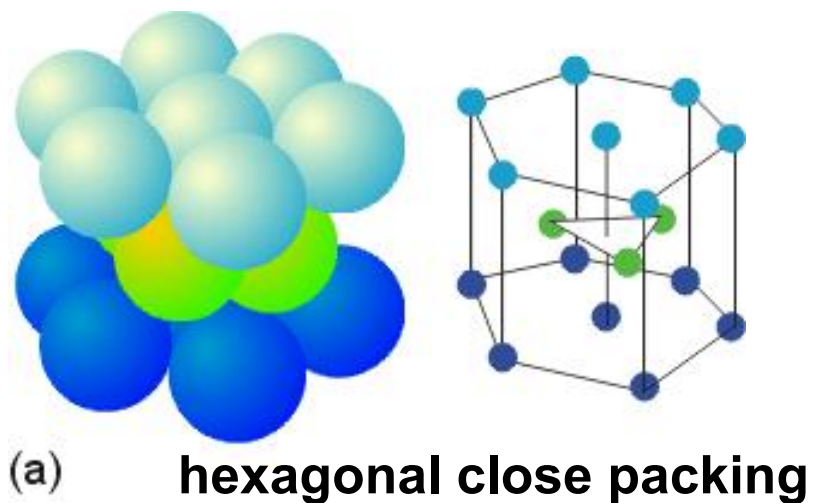
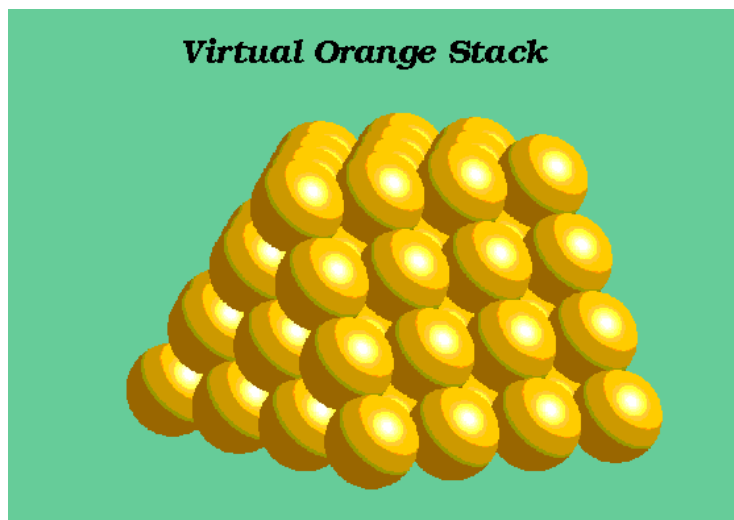




# How structures are made

Anions always are the largest spheres, they build a closed packed lattice

In oxides:  $O^{2-}$



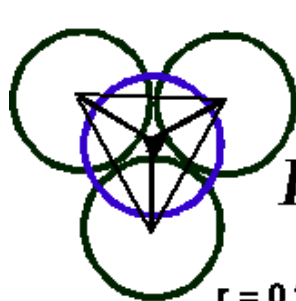
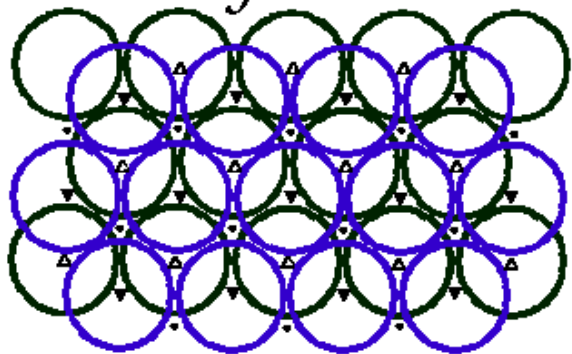


# How structures are made: holes

Anions always are the largest spheres, they build a closed packed lattice

Cations are stuffed in the holes

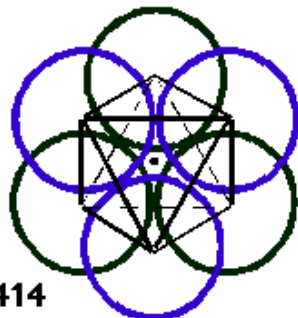
*2 layers*



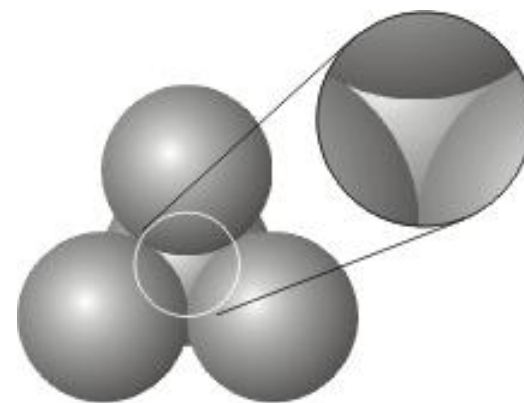
*Holes*

$r = 0.225$     $r = 0.414$

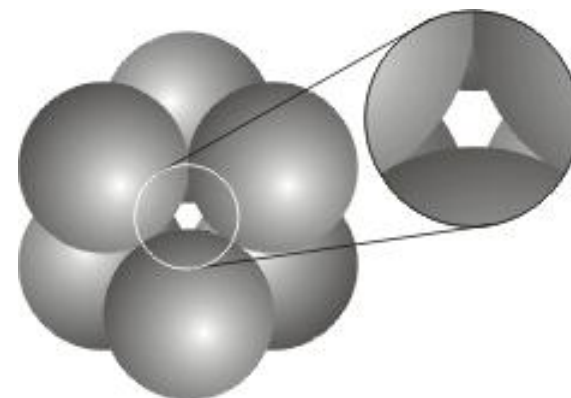
**Tetrahedral**



**Octahedral**



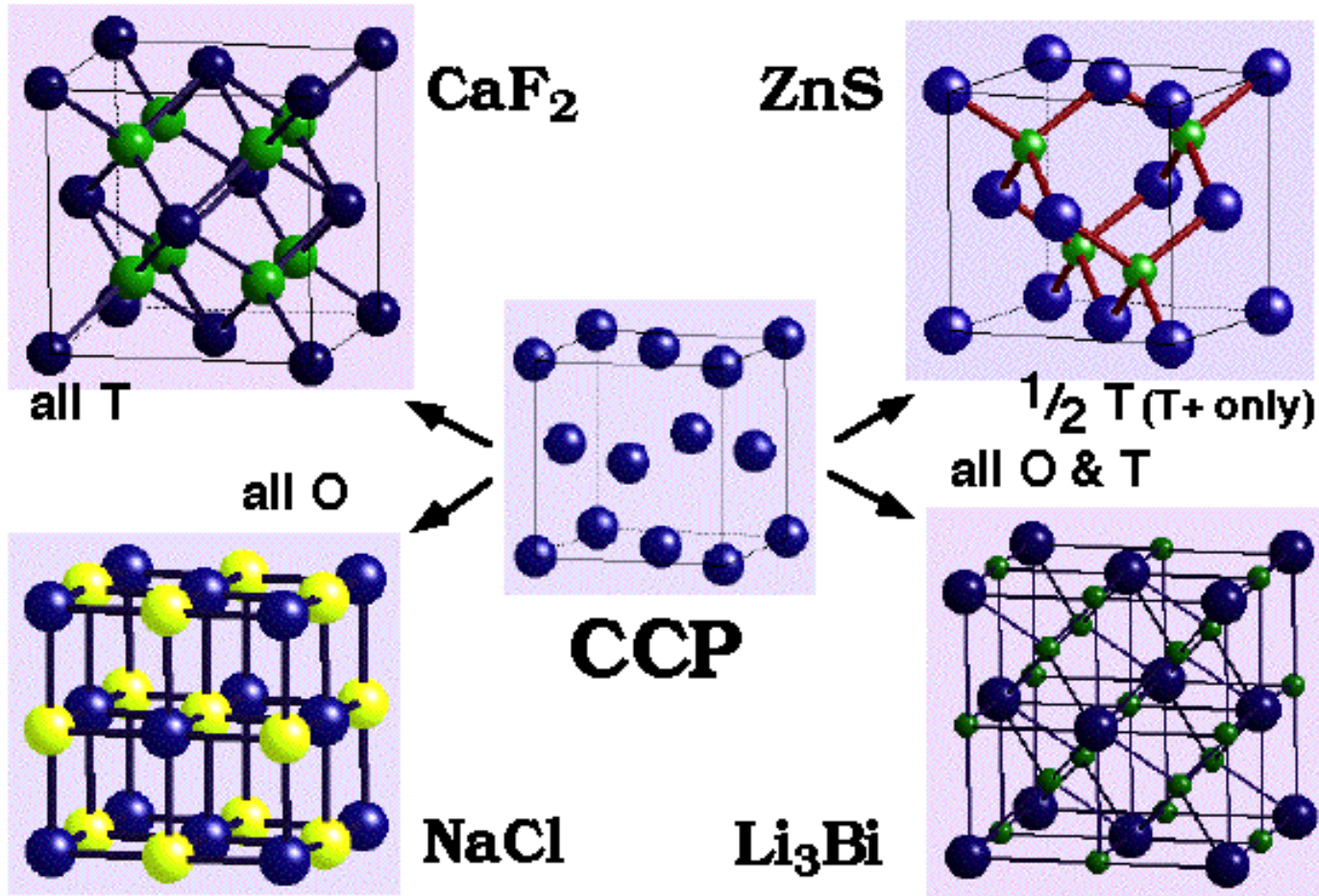
**5** Tetrahedral hole



**2** Octahedral hole



# Simple ionic structures

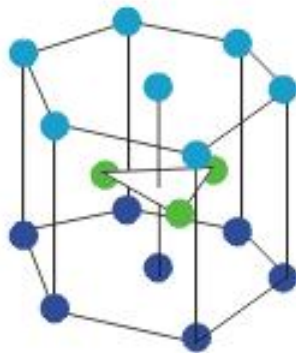




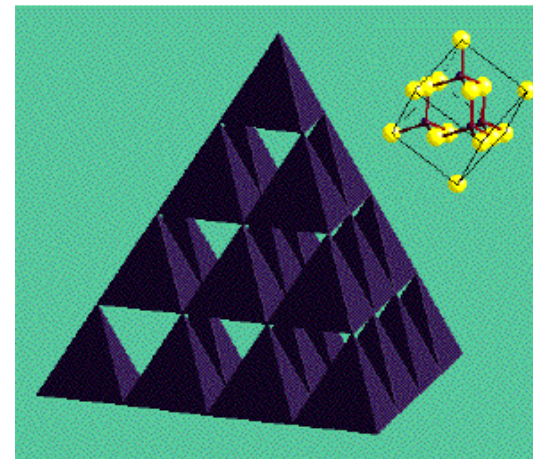
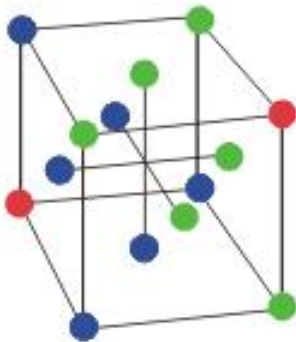
# Filled voids in the hexagonal lattice



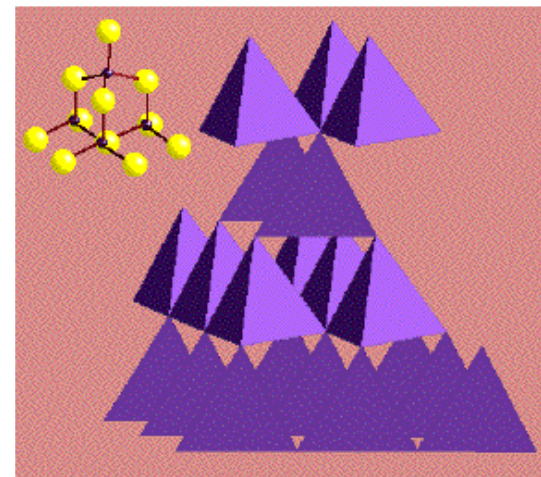
(a)



(b)



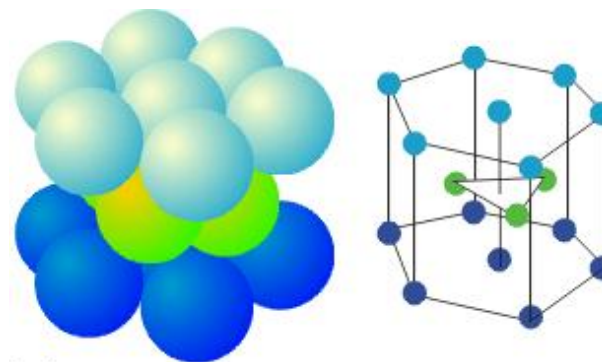
Zinc Blende



Wurtzite

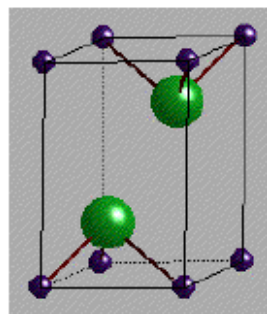
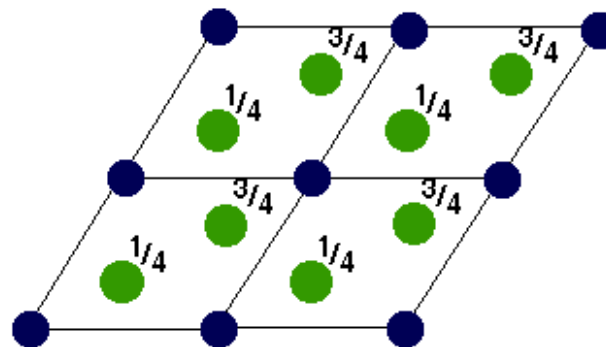
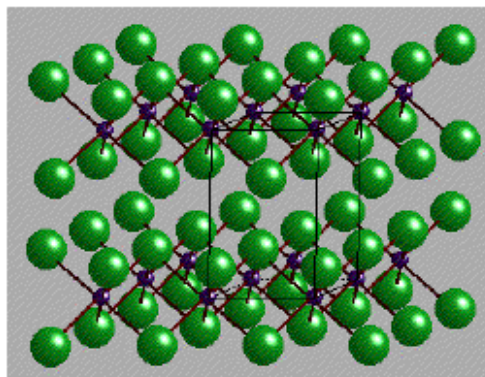
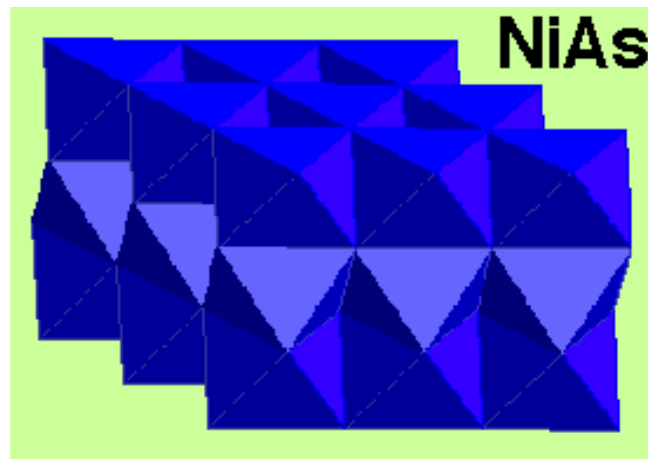
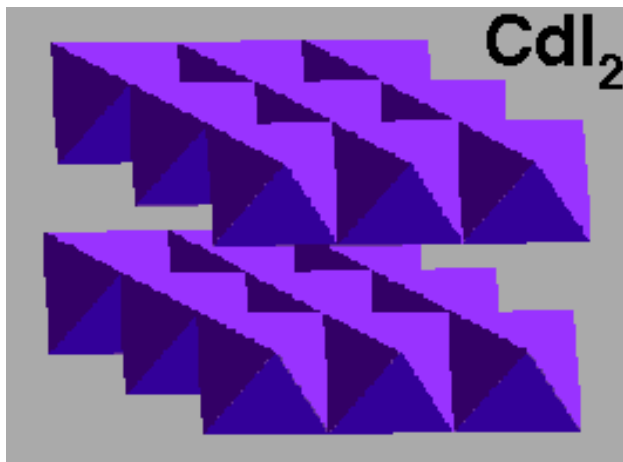


Formula	Type/fraction of sites occ.	HCP	CCP
AB	All octahedral	NiAs Nickel Arsenide	NaCl Rock Salt
	Half tetrahedral	ZnS Wurtzite	ZnS Zinc Blende
A <sub>2</sub> B	All tetrahedral	Not known	CaF <sub>2</sub> /Mg <sub>2</sub> Si (Fluorite/Anti-Fluorite)
A <sub>3</sub> B	All octahedral & tetrahedral	Not known	Li <sub>3</sub> Bi

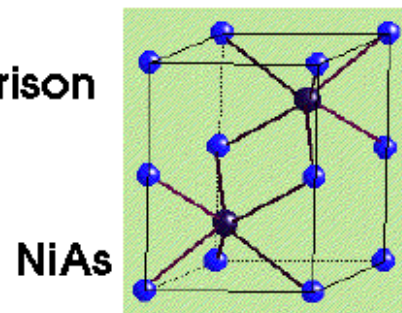




# Layered structure



Comparison  
CdI<sub>2</sub> vs

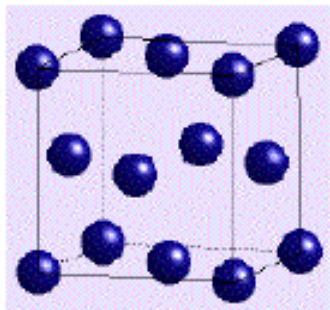




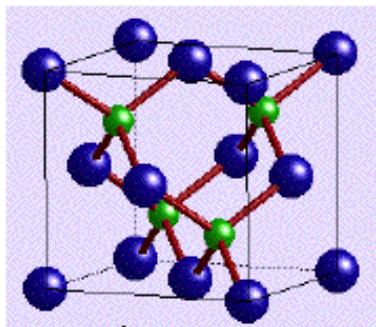
Formula	Type/fraction of sites occ.	HCP	CCP
AB	All octahedral	NiAs Nickel Arsenide	NaCl Rock Salt
	Half tetrahedral	ZnS Wurtzite	ZnS Zinc Blende
A <sub>2</sub> B	All tetrahedral	Not known	CaF <sub>2</sub> /Mg <sub>2</sub> Si (Fluorite/Anti-Fluorite)
A <sub>3</sub> B	All octahedral & tetrahedral	Not known	Li <sub>3</sub> Bi
AB <sub>2</sub>	Half octahedral (Alternate layers full/empty)	CdI <sub>2</sub> Cadmium Chloride	CdCl <sub>2</sub> Cadmium Chloride
	Half octahedral (ordered framework arrangement)	CaCl <sub>2</sub> TiO <sub>2</sub> (Rutile)	TiO <sub>2</sub> (Anatase)
AB <sub>3</sub>	1/3 octahedral Alternate layers 2/3 empty	BiI <sub>3</sub>	AlCl <sub>3</sub>
A <sub>2</sub> B <sub>3</sub>	2/3 octahedral (Ordered framework)	Al <sub>2</sub> O <sub>3</sub> /FeTiO <sub>3</sub> Corundum/Ilmenite	



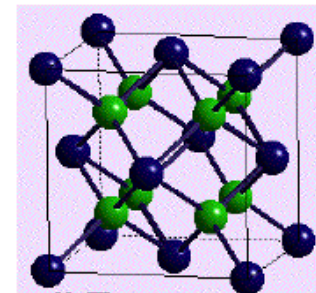
# Filled fcc



**CCP**

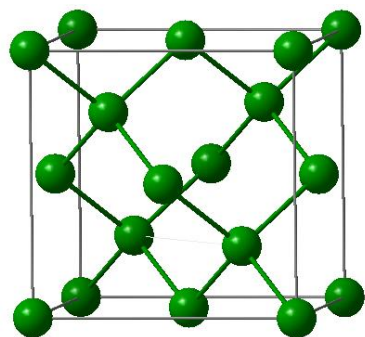


$\frac{1}{2}$  T (T+ only)

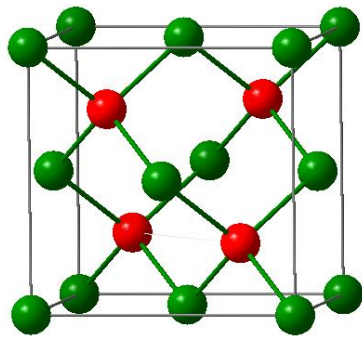


all T

**Diamond**

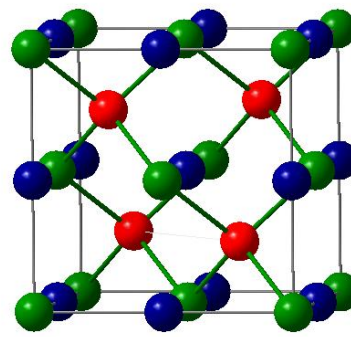


**ZnS**



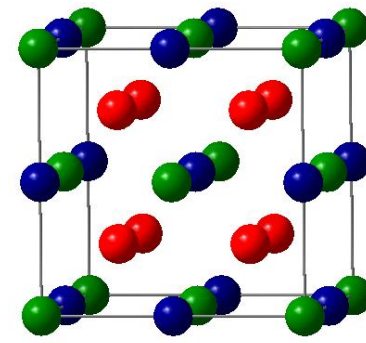
2 interpenetrating fcc  
with half of the tetrahedral  
sites filled

**Heusler XYZ C1<sub>b</sub>**



3 interpenetrating fcc  
half of the tetrahedral sites  
and the octahedral sites

**X<sub>2</sub>YZ L2<sub>1</sub>**



4 interpenetrating fcc  
all tetrahedral sites filled  
and the octahedral sites



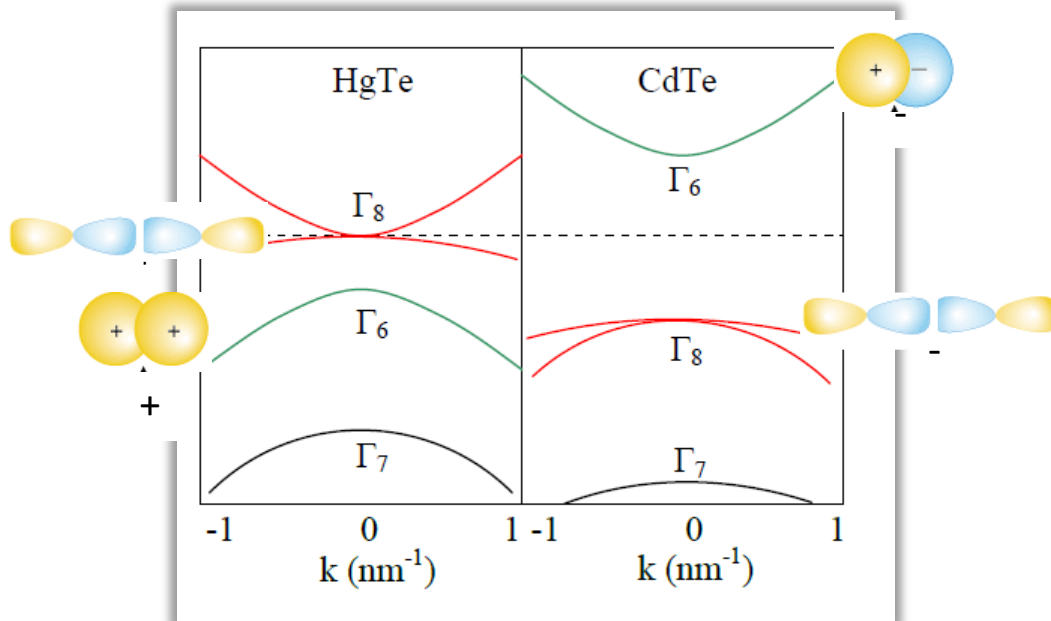


# Quantum Spin Hall



## Quantum Spin Hall Effect and Topological Phase Transition in HgTe Quantum Wells

B. Andrei Bernevig, *et al.*  
*Science* **314**, 1757 (2006);  
DOI: 10.1126/science.1133734

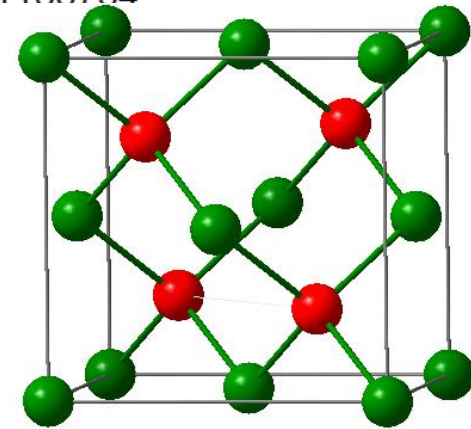


### Inert pair effect

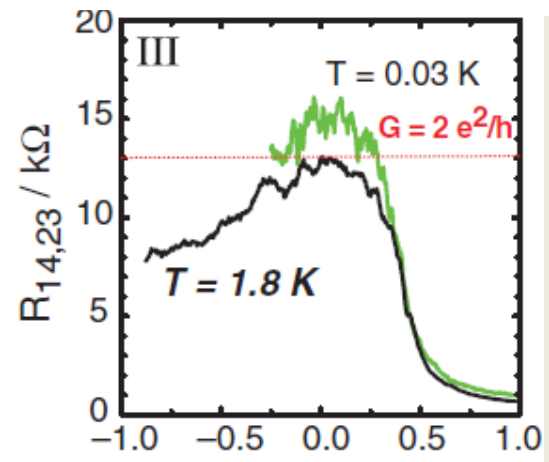
Bernevig, *et al.*, *Science* 314, 1757 (2006)

Bernevig, S.C. Zhang, *PRL* 96, 106802 (2006)

König, *et al.* *Science* 318, 766 (2007)



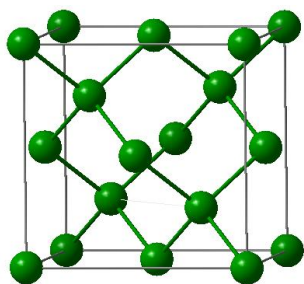
3D: Dirac cone on the surface  
2D: Dirac cone in quantum well



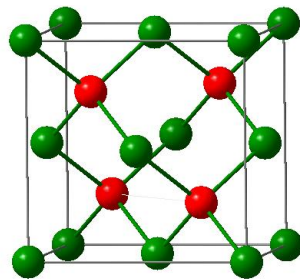


# Heusler compounds

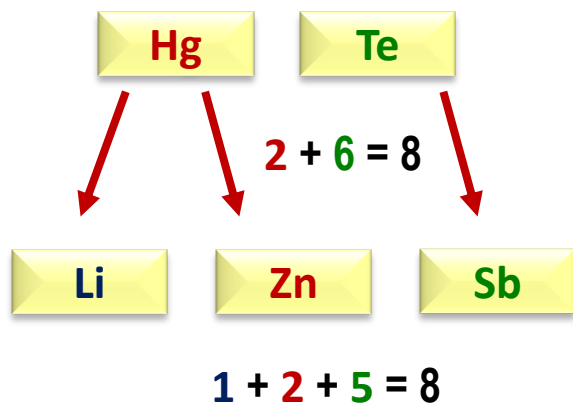
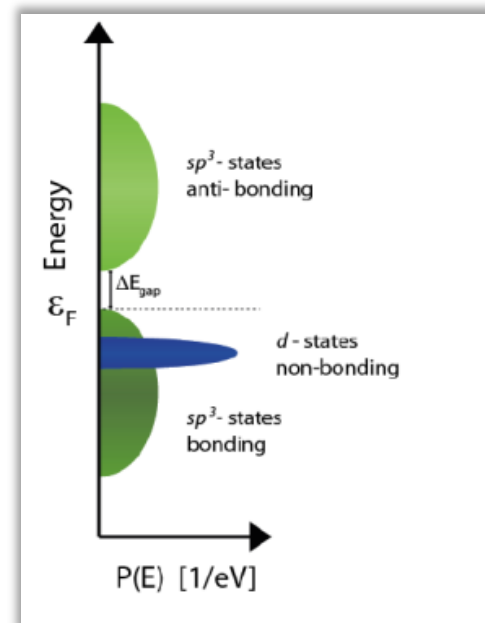
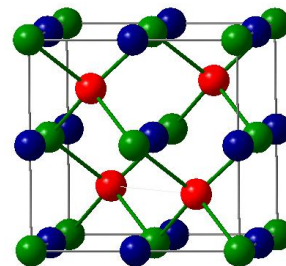
Diamond



ZnS



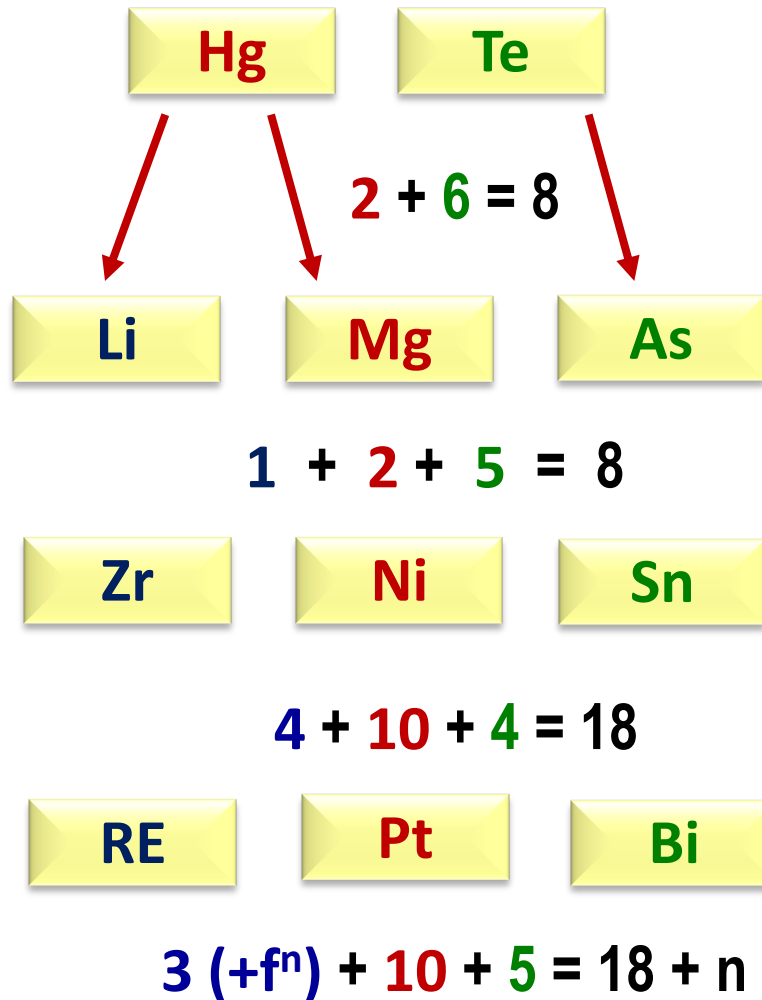
Heusler XYZ C1<sub>b</sub>



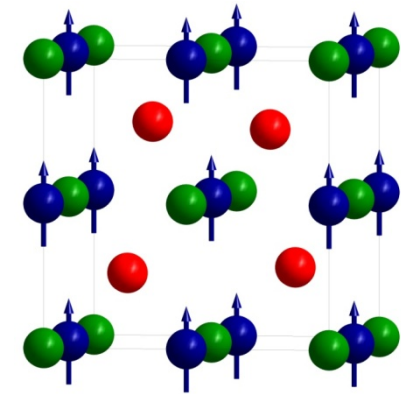


# Counting electrons

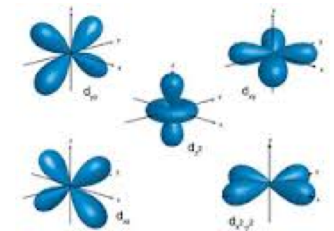
From wide to low band gap semiconductor



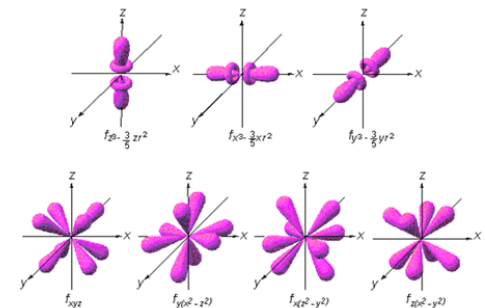
2 s  
6 p



10 d

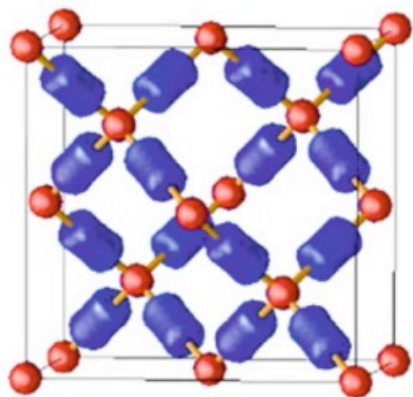


14 f

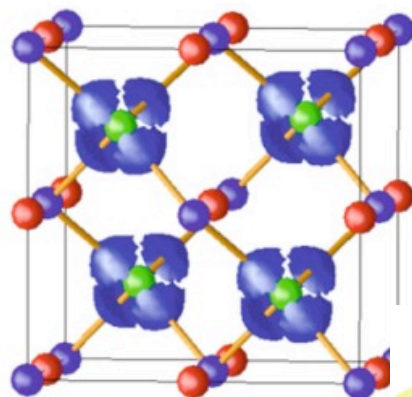




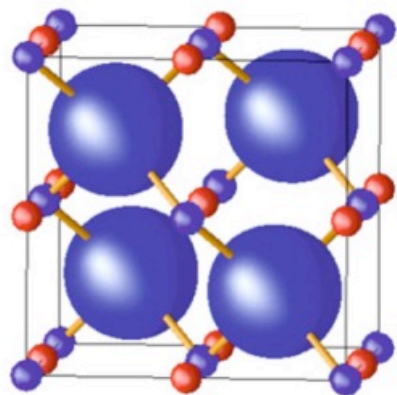
# Ionic and covalent structure



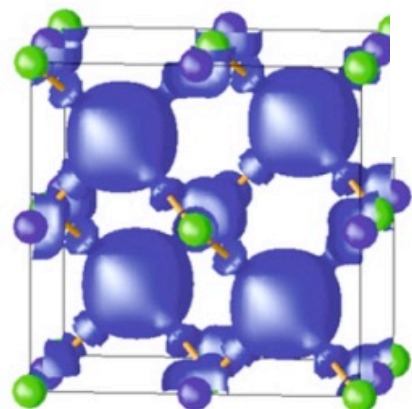
Si



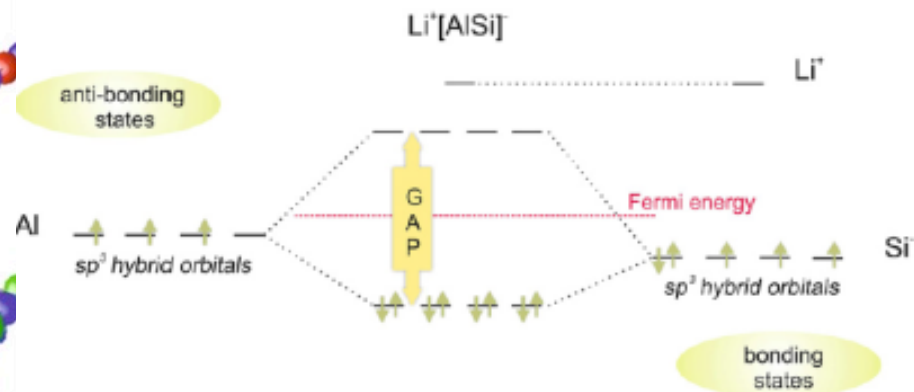
LiAlSi



LiMgN

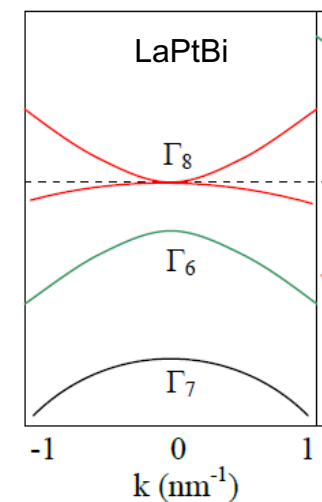
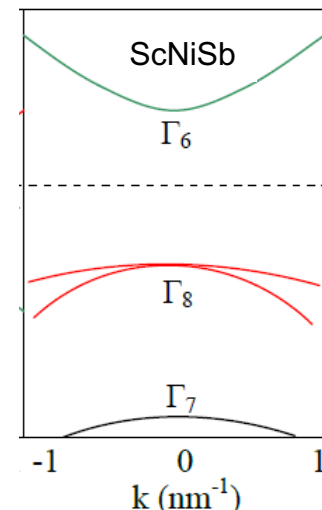
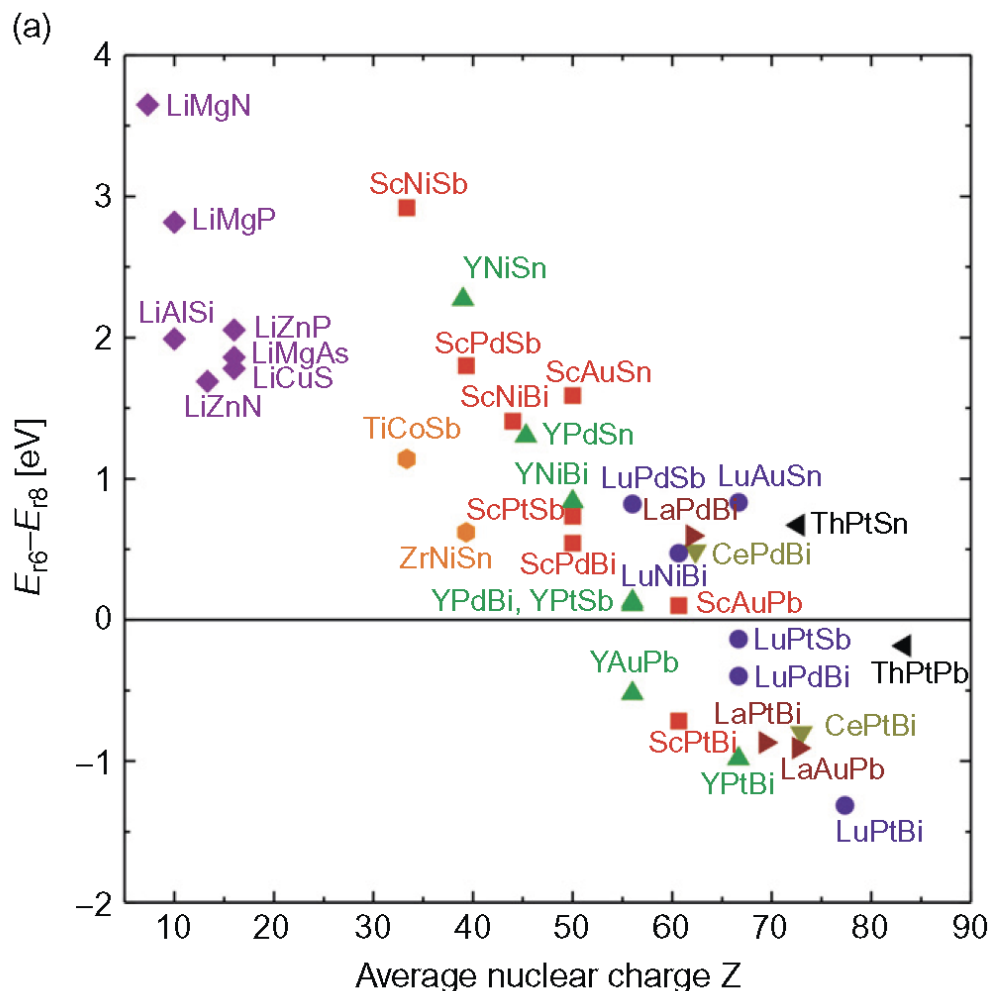
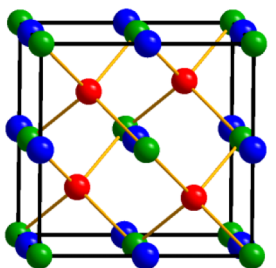
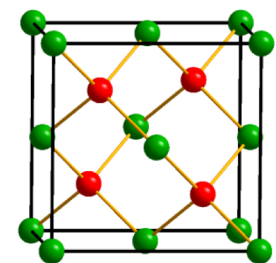


TiCoSb





# Predicting topological insulators



S. Chadov et al., Nat. Mater. 9 541 (2010).

H. Lin et al., Nat. Mater. 9 546 (2010).



# From Orbitals to Bands

## How Chemistry and Physics Meet in the Solid State

By **Roald Hoffmann\***

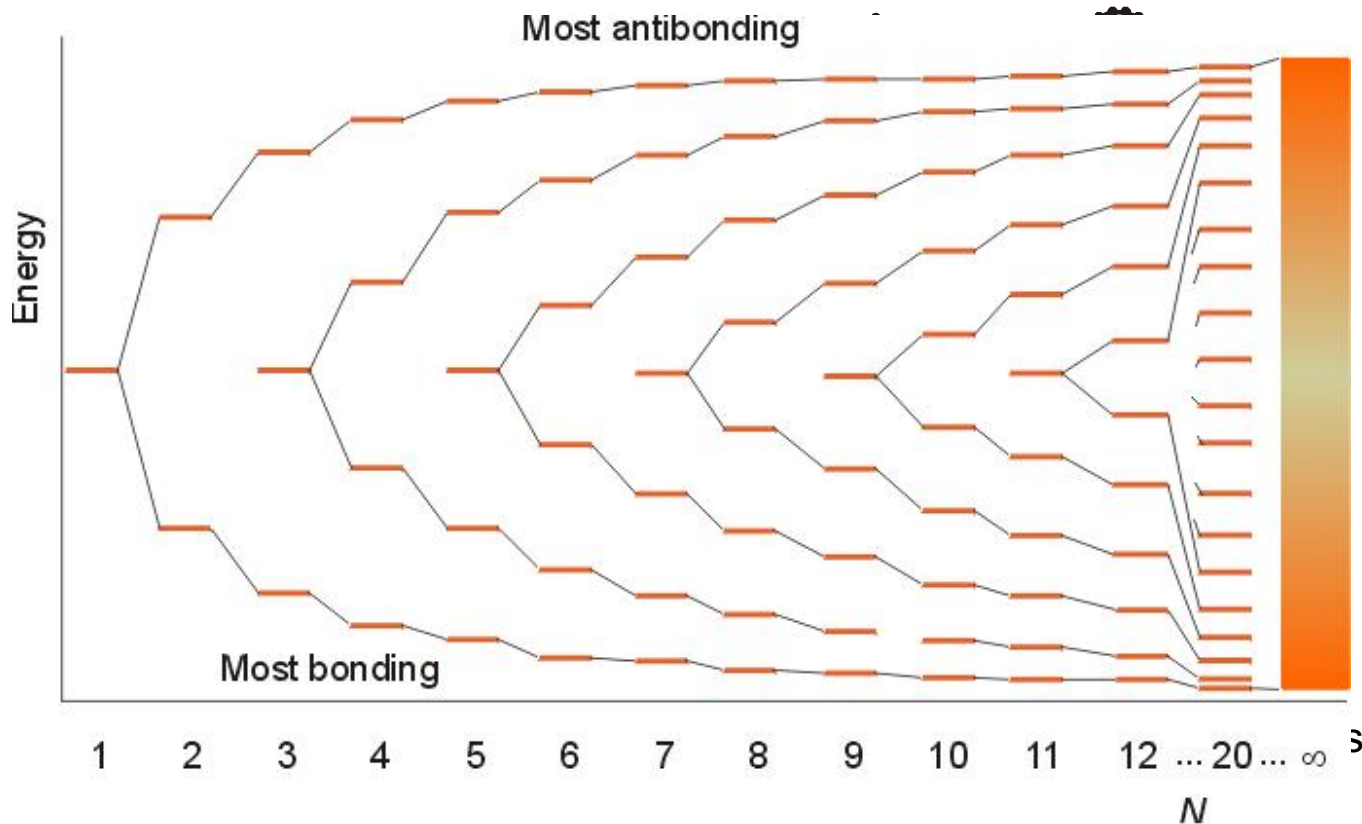
Hoffmann *Angewandte. Chem.* 26 (1987) 846

Energy bands in solids arise from overlapping atomic orbitals

⇒ crystal orbitals (which make up the bands)

Recipe: use LCAO (tight binding) approach

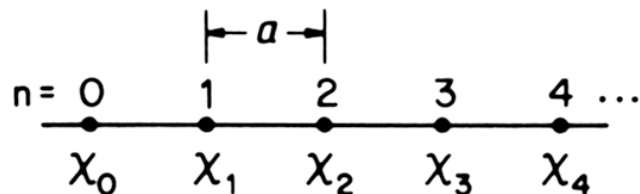
Crystal = regular periodic array ⇒ translational symmetry





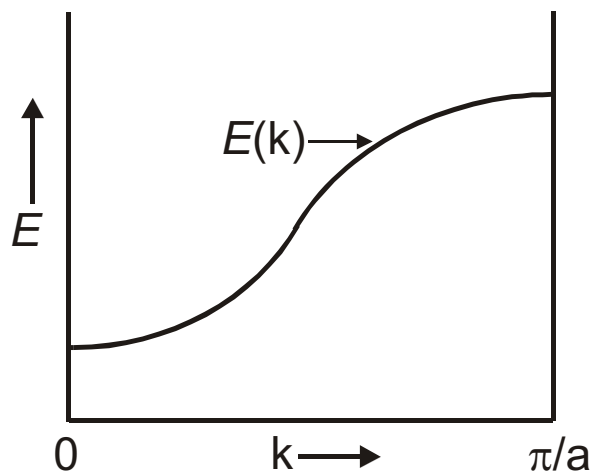
# How to find a band structure

We start from atomic orbitals – localized picture: linear chain of hydrogen atoms  
Using the translational symmetry of the solid we can set up the  $n$  terms of symmetry with a 1s basis function for two special values of  $k$



$$\psi_k = \sum_n e^{ikna} \chi_n$$

Test with a 1s basis function for two special values of  $k$



$$k = 0 \quad \Psi_0 = \sum_n e^{i0n} \chi_n = \sum_n \chi_n = \chi_0 + \chi_1 + \chi_2 + \chi_3 \dots$$



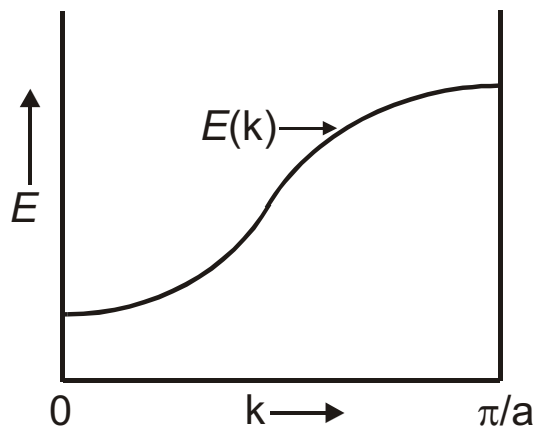
$$k = \frac{\pi}{a} \quad \Psi_{\frac{\pi}{a}} = \sum_n e^{i\pi n} \chi_n = \sum_n (-1)^n \chi_n = \chi_0 - \chi_1 + \chi_2 - \chi_3 \dots$$





# How to find a band structure

The topology of the orbital interaction determines how a band runs



$$k = 0 \quad \Psi_0 = \sum_n e^{i0n} \chi_n = \sum_n \chi_n = \chi_0 + \chi_1 + \chi_2 + \chi_3 \dots$$



$$k = \frac{\pi}{a} \quad \Psi_{\frac{\pi}{a}} = \sum_n e^{i\pi n} \chi_n = \sum_n (-1)^n \chi_n = \chi_0 - \chi_1 + \chi_2 - \chi_3 \dots$$



$k = 0$  bonding interaction  $\Rightarrow$  band runs „uphill“

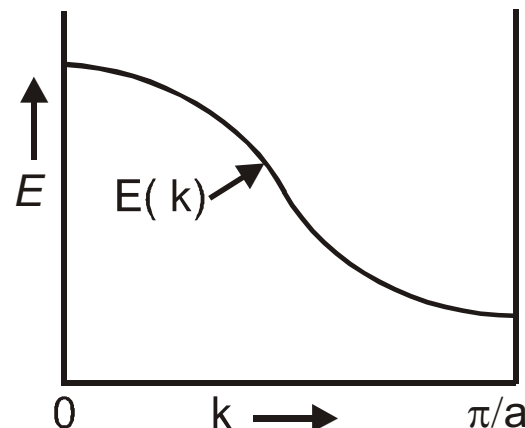
$$\Psi_0 = \chi_0 + \chi_1 + \chi_2 + \chi_3 + \dots$$



$$\Psi_{\frac{\pi}{a}} = \chi_0 - \chi_1 + \chi_2 - \chi_3 + \dots$$



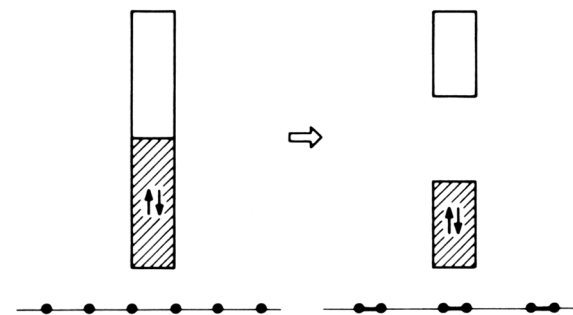
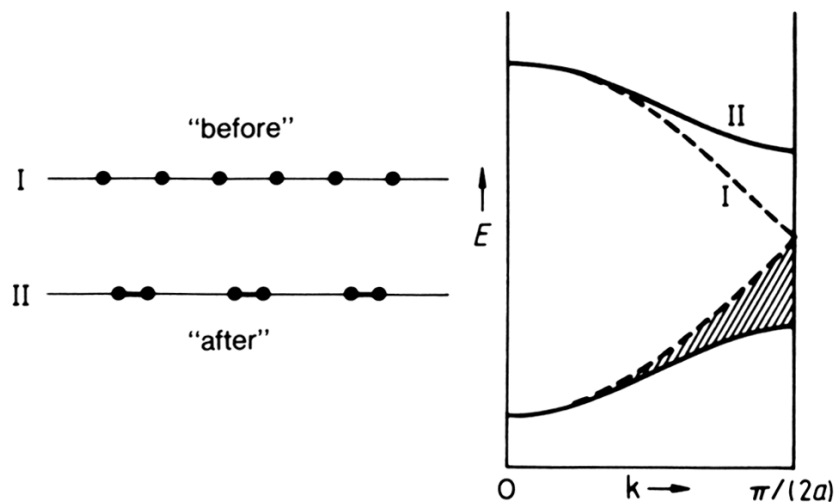
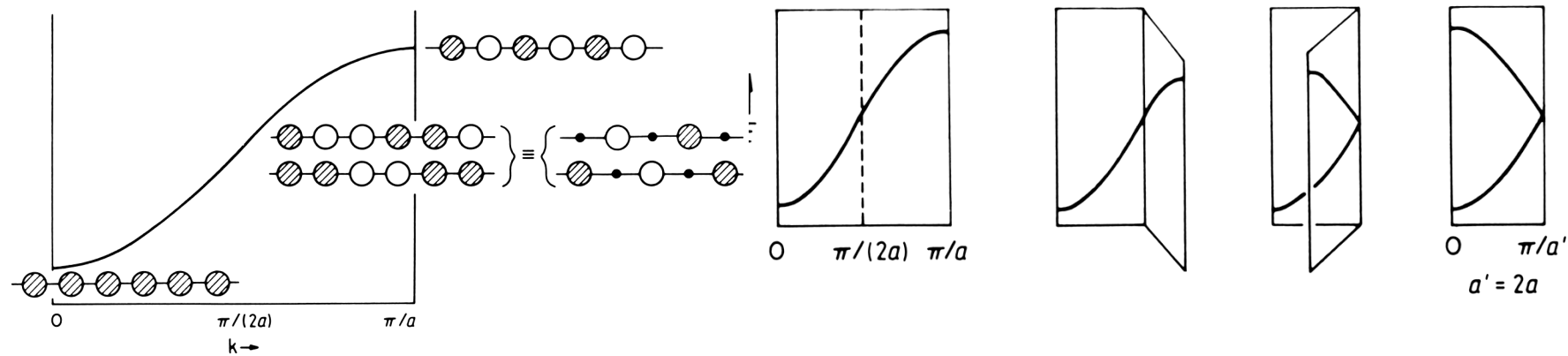
$k = 0$  antibonding interaction  $\Rightarrow$  band runs „downhill“







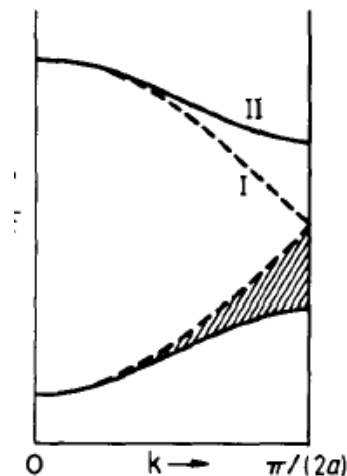
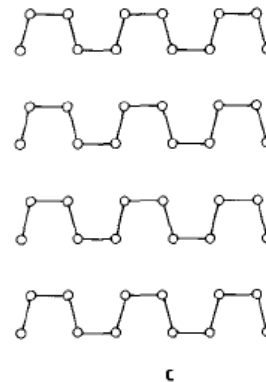
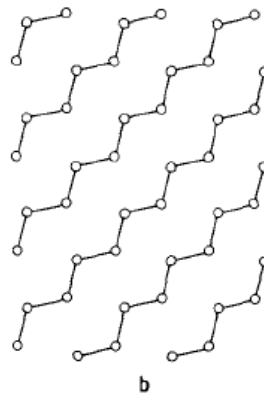
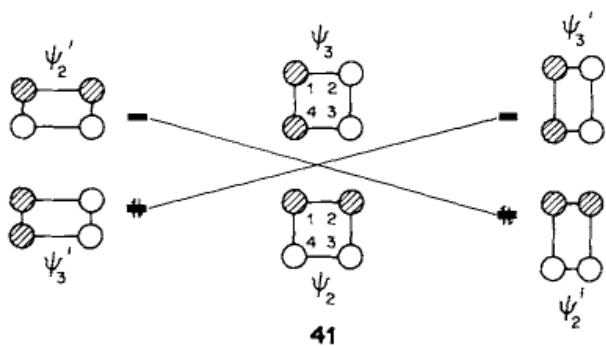
# Why is Hydrogen a molecule



## Peierls Distortion



# Square nets



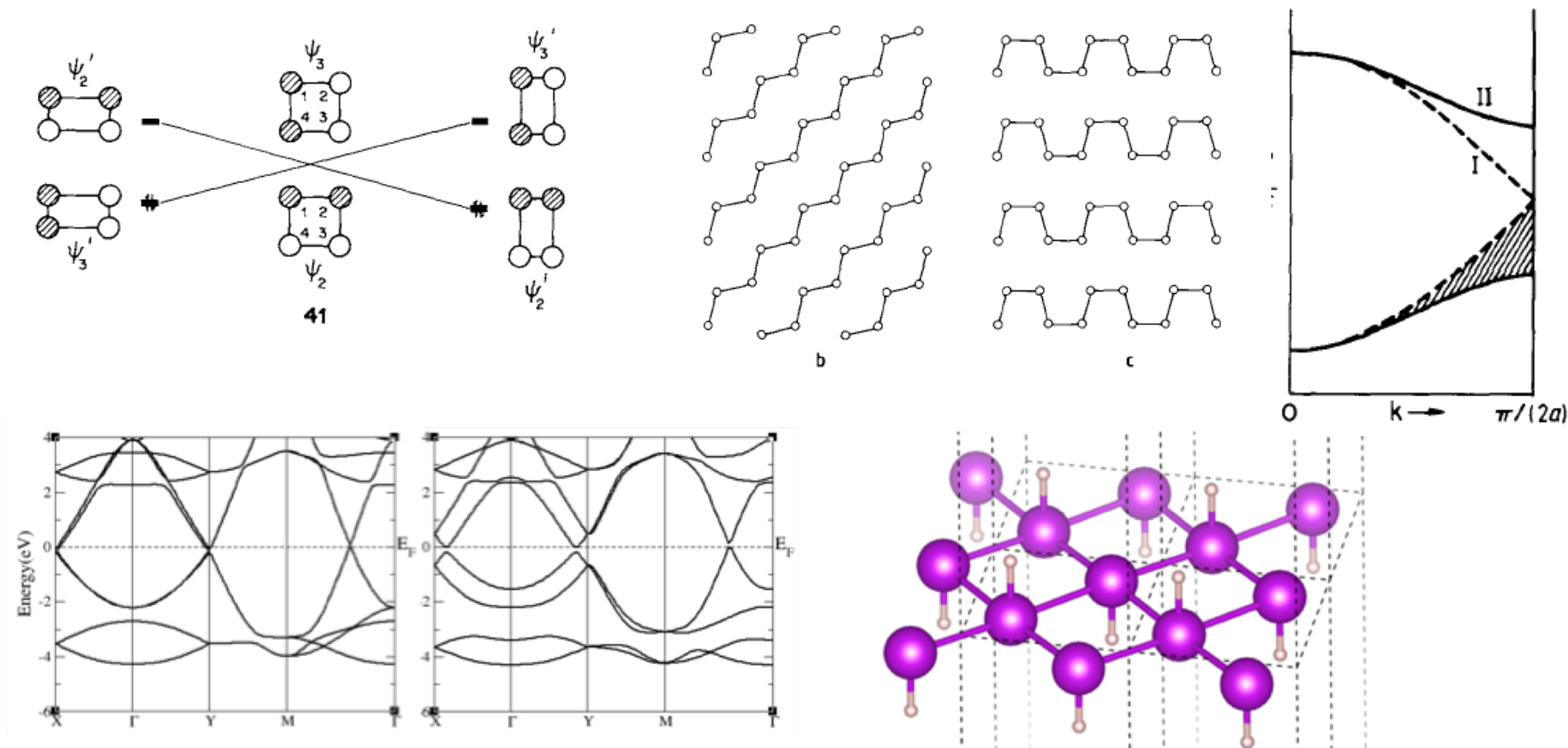
## Square Nets of Main Group Elements in Solid-State Materials

Wolfgang Tremel<sup>1</sup> and Roald Hoffmann\*

*Contribution from the Department of Chemistry and Materials Science Center, Cornell University, Ithaca, New York 14853. Received May 29, 1986*



# Square nets of electron doped Bi

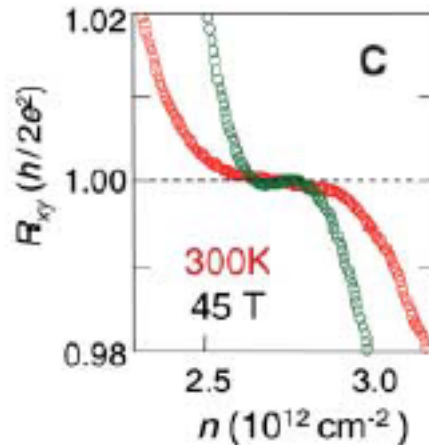
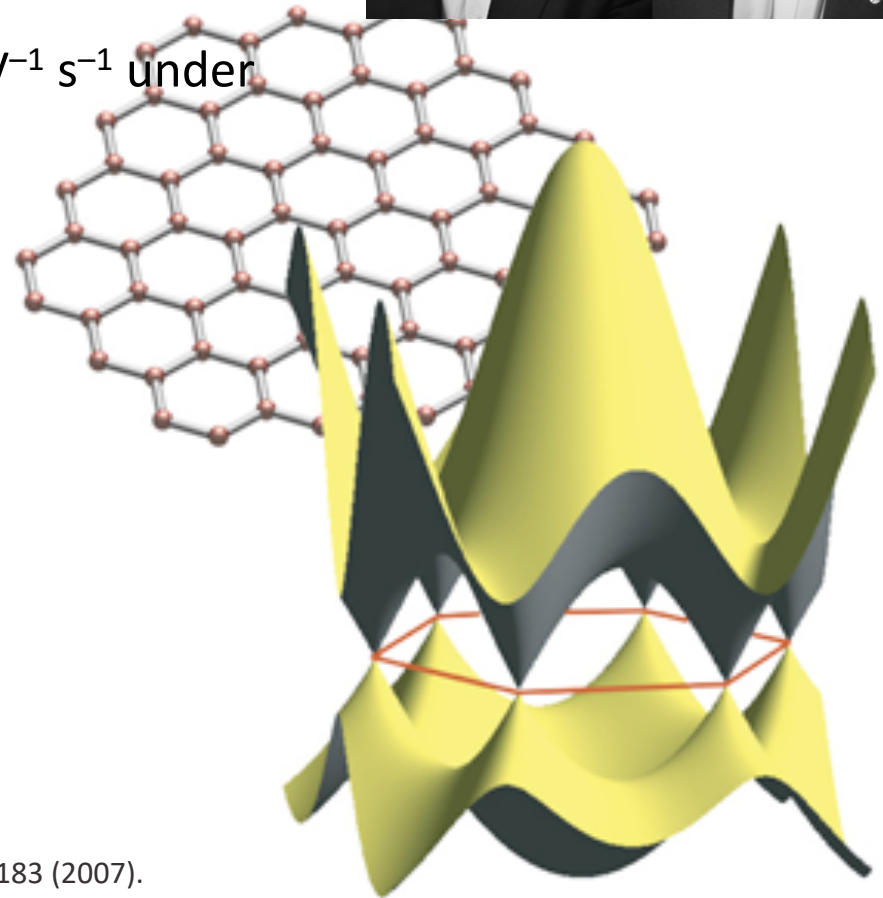


- Neither the valence nor conduction bands form a band representation  $\rightarrow$  topological (in this case, 2d QSH)
- Group 129, 139



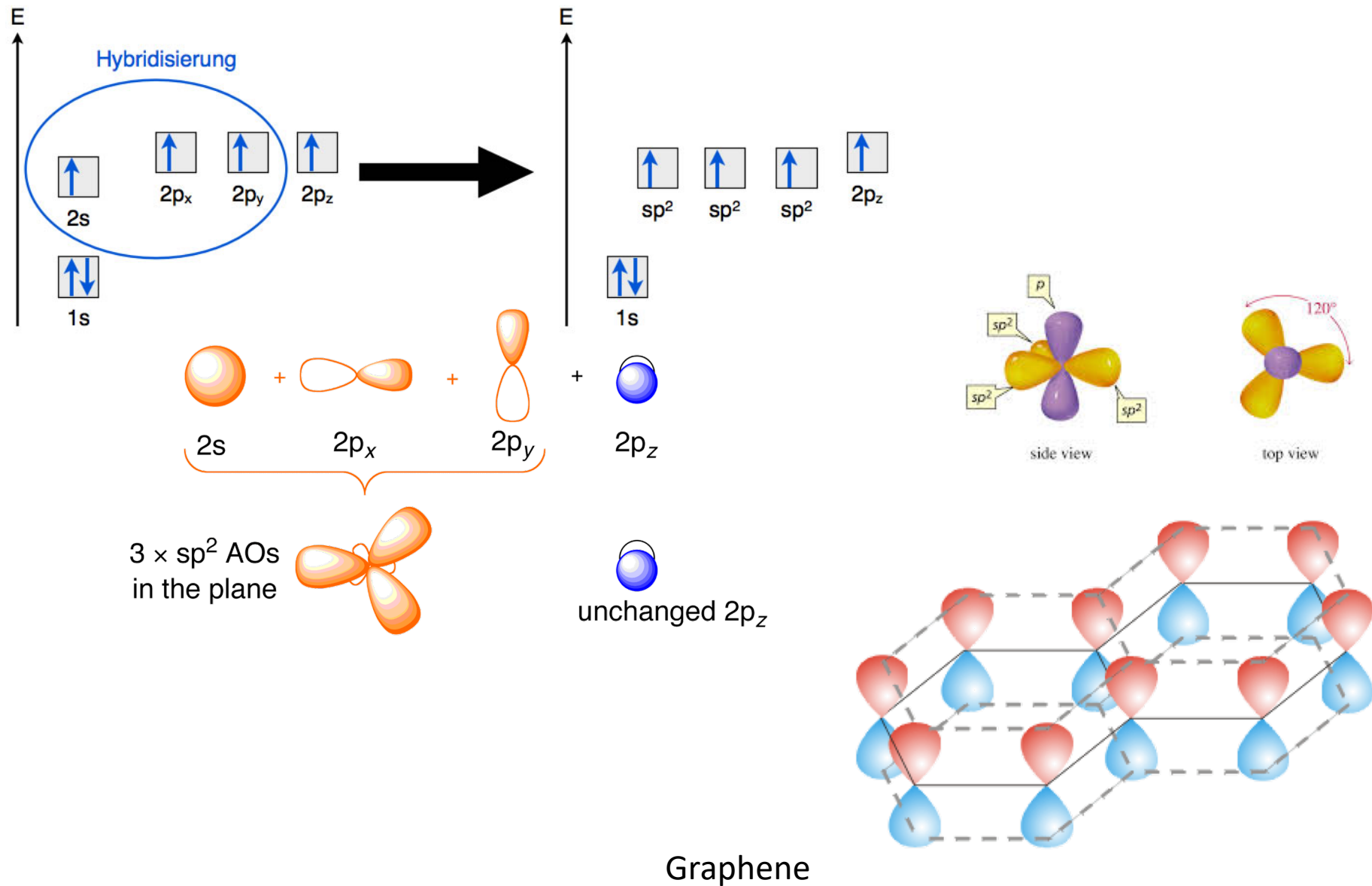
# Graphene

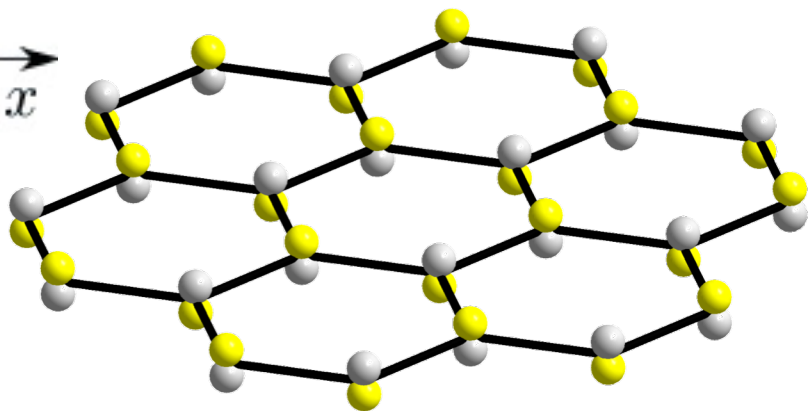
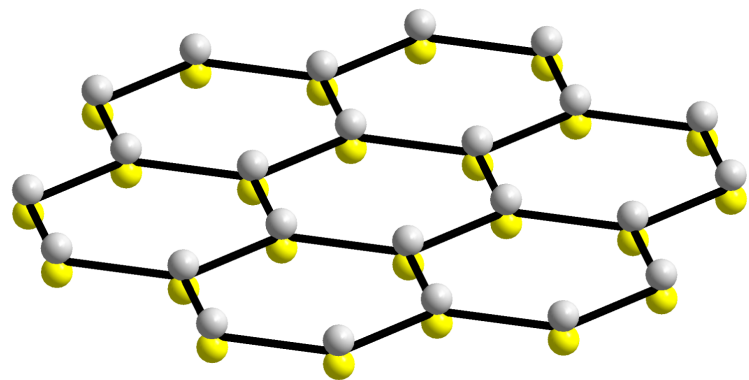
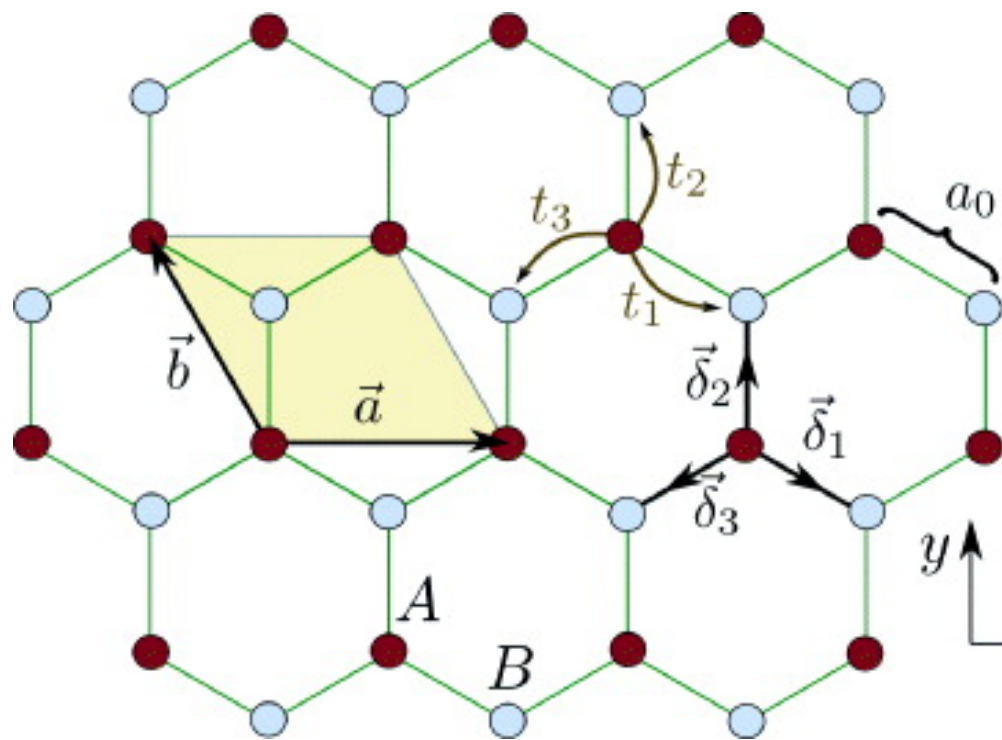
- Graphene's conductivity exhibits values close to the conductivity quantum  $e^2/h$  per carrier type
- Graphene's charge carriers can be tuned continuously between electrons and holes in concentrations  $n = 10^{13} \text{ cm}^{-2}$
- Mobilities  $\mu$  can exceed  $15,000 \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1}$  under ambient conditions
- InSb has  $\mu \approx 77,000 \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1}$





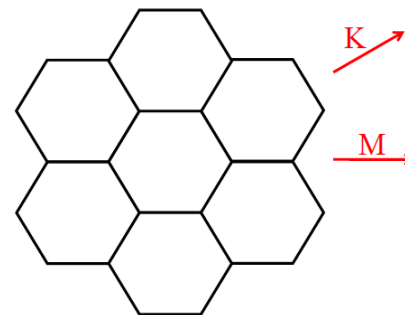
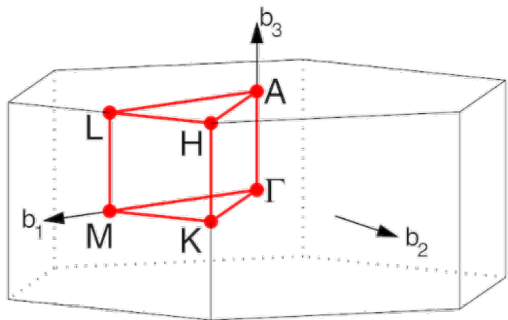
# sp<sup>2</sup>-Hybrid





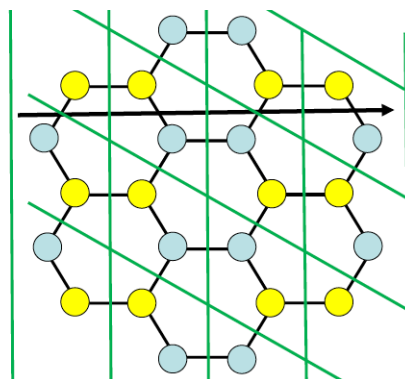
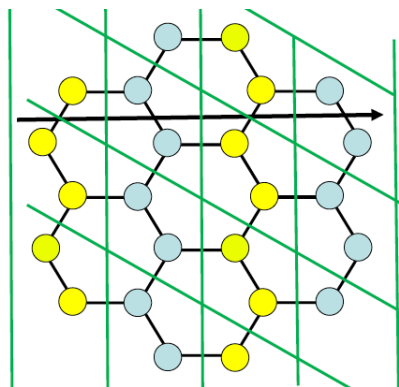
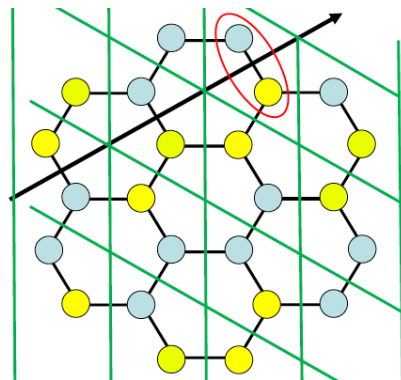
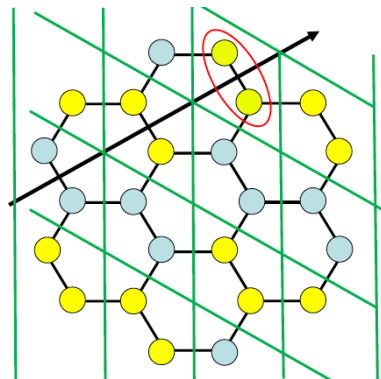


# Graphene



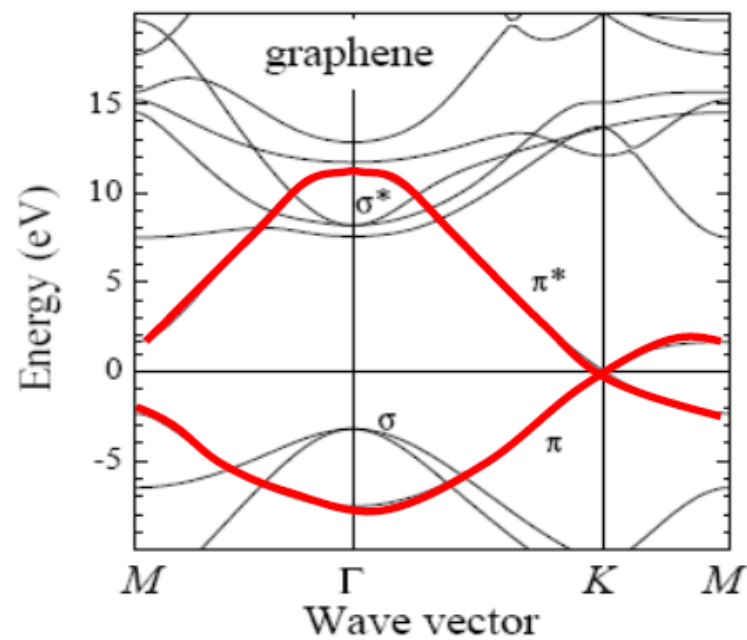
$p_z, \pi, K$ : non-bonding

$p_z, \pi^*, K$ : non-bonding



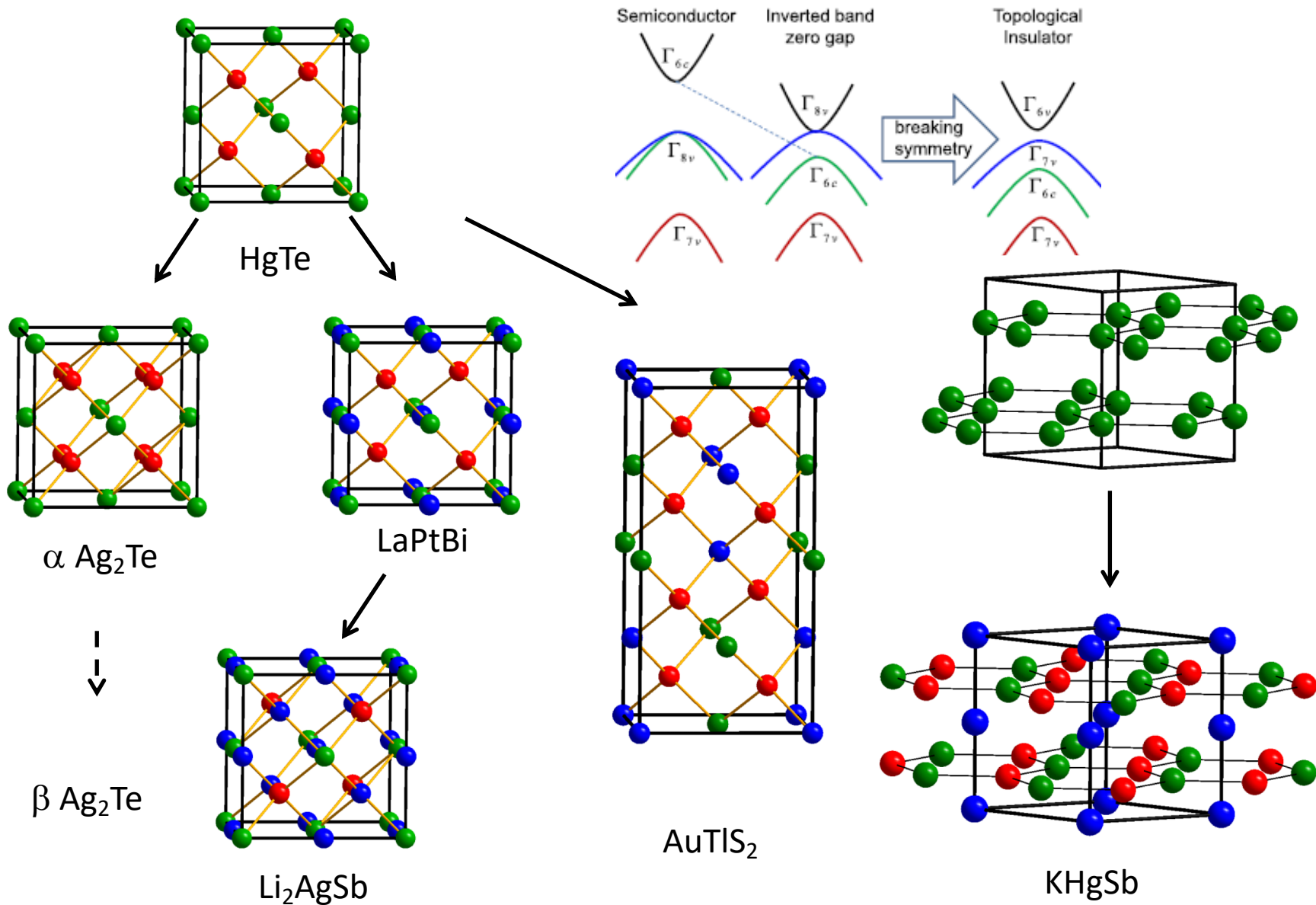
$p_z, \pi, M$ : bonding

$p_z, \pi, M^*$ : anti-bonding





# Structure to Property

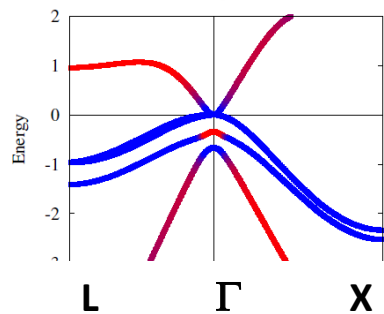




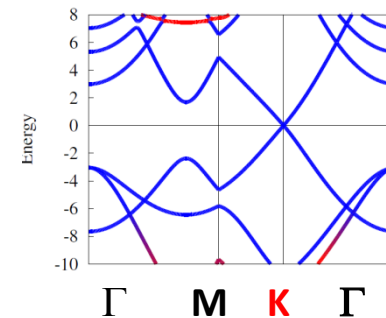


# Struktur und elektronische Struktur

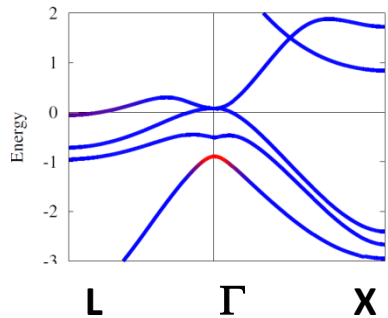
### HgTe



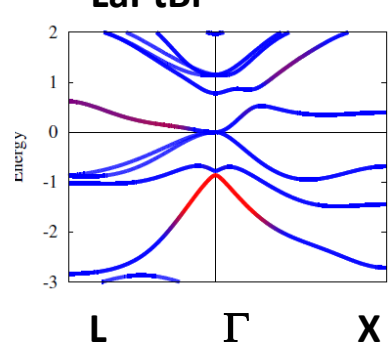
### Graphite



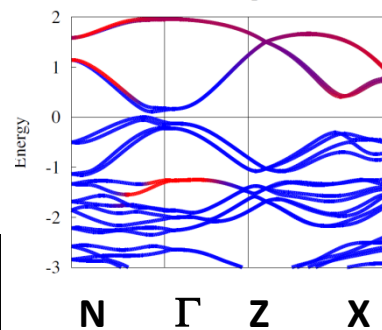
### $\alpha$ Ag<sub>2</sub>Te



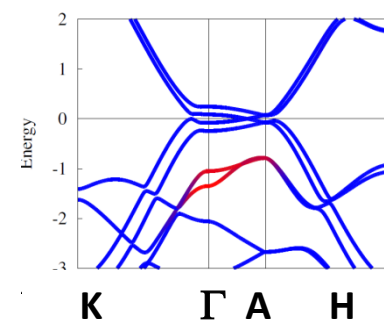
### LaPtBi



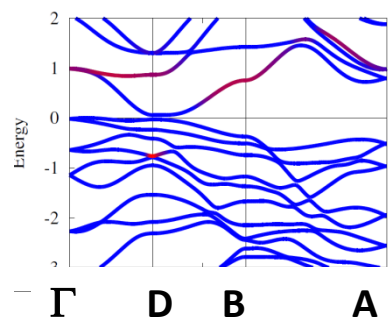
### AuTeTe<sub>2</sub>



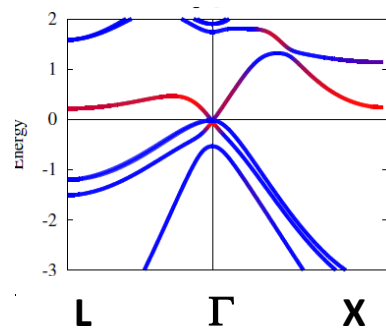
### LiAuTe



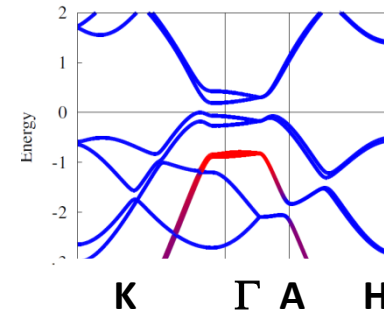
### $\beta$ Ag<sub>2</sub>Te



### Li<sub>2</sub>AgSb



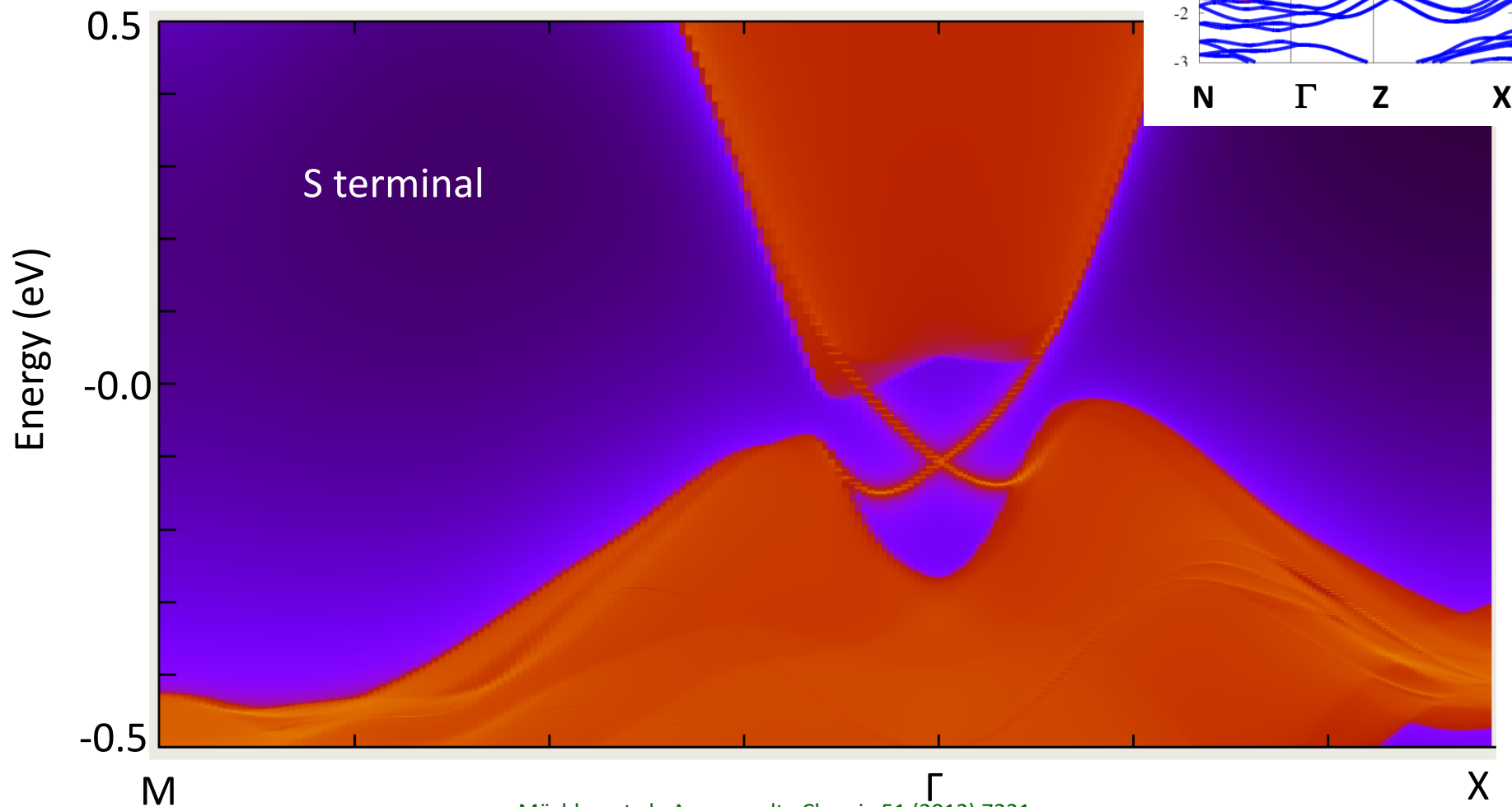
### KHgSb





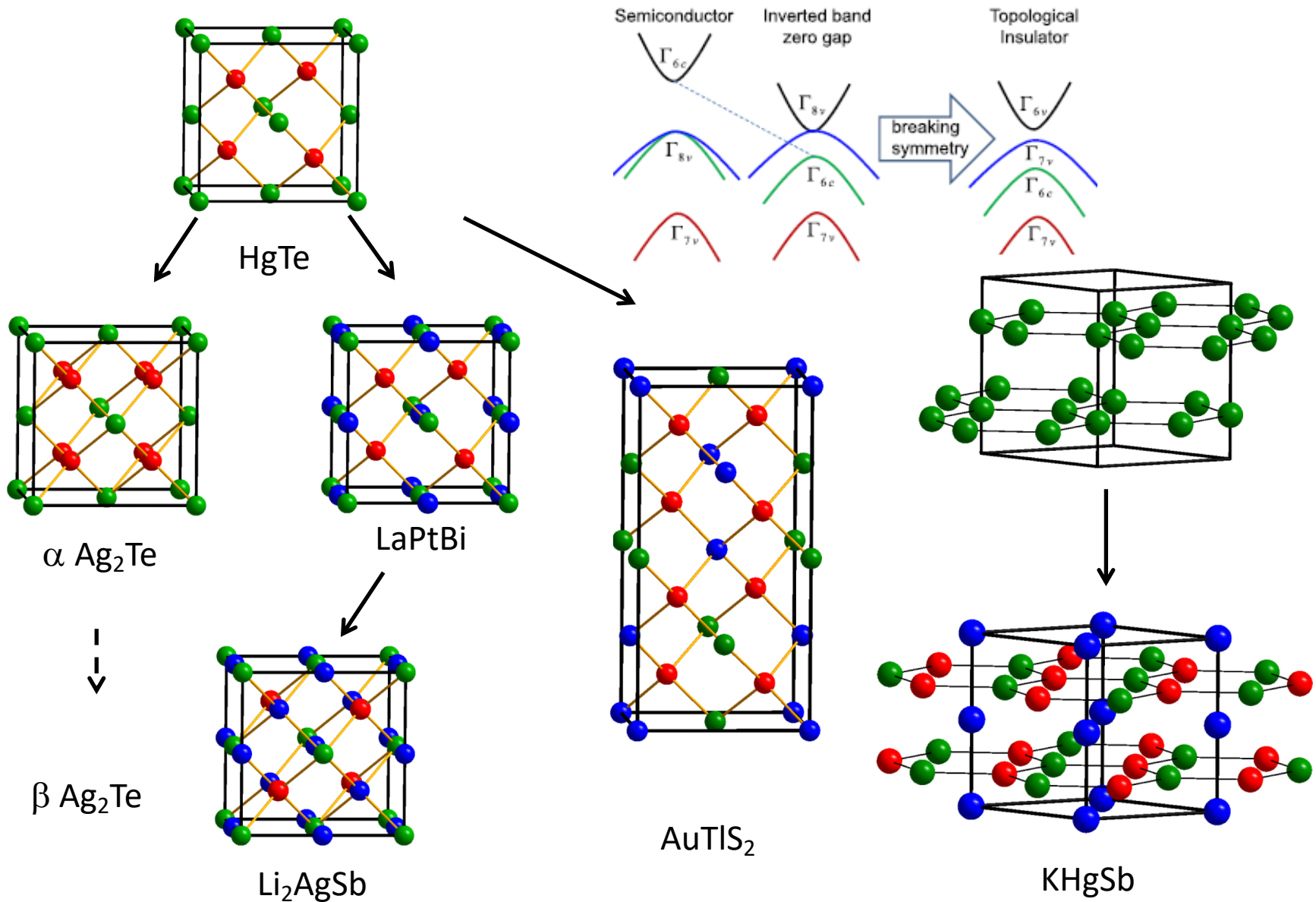
# Structure and electronic structure

## AuTe<sub>2</sub>



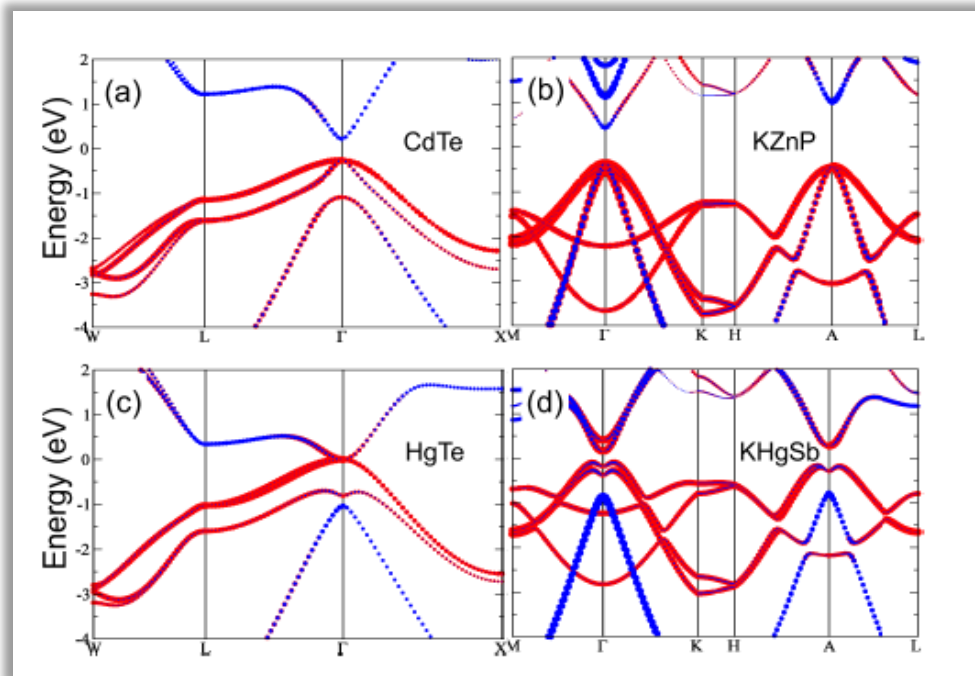
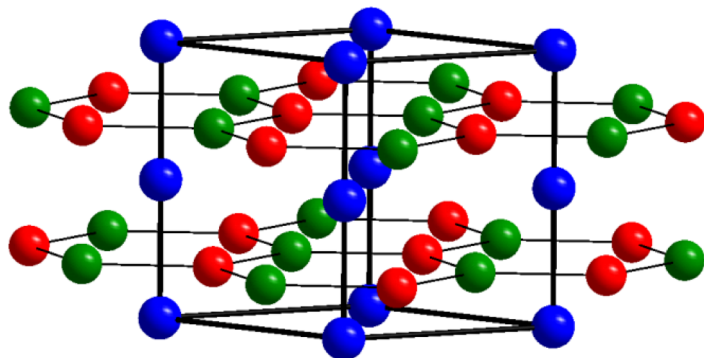


# Structure to Property





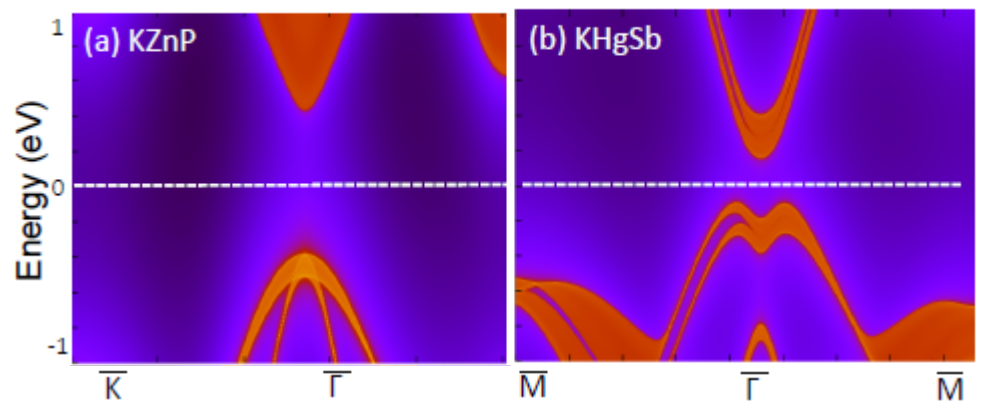
# Honeycomb from $sp^3$ to $sp^2$



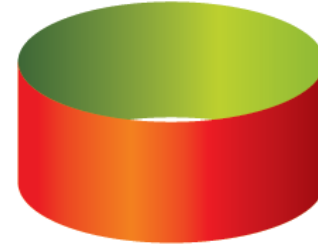
Band inversion is found in the heavier compounds

No surface state? Why ?

➔ Interaction between the two layers in the unit cell and two Dirac Cones



a)

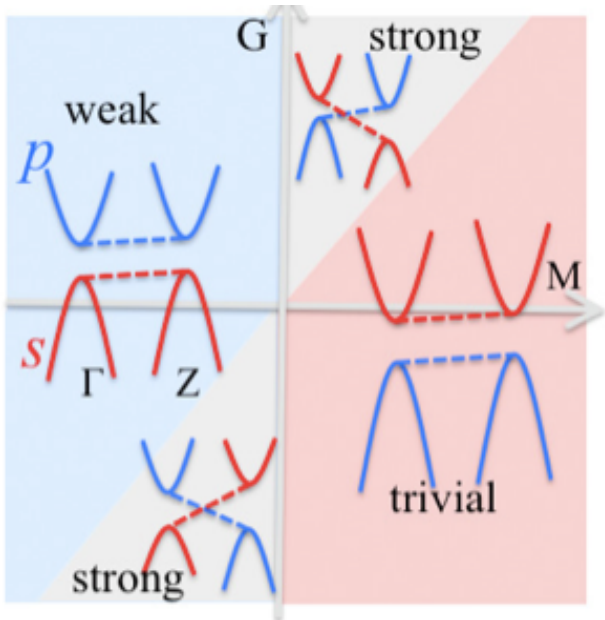
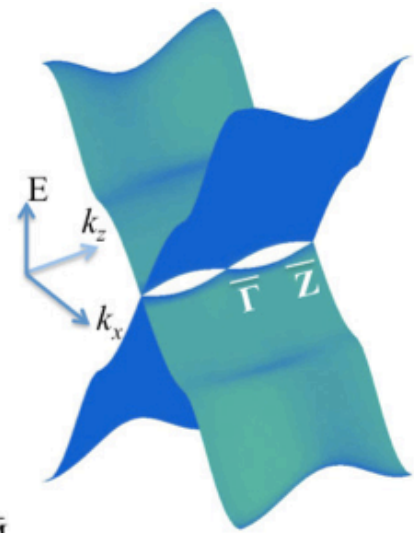
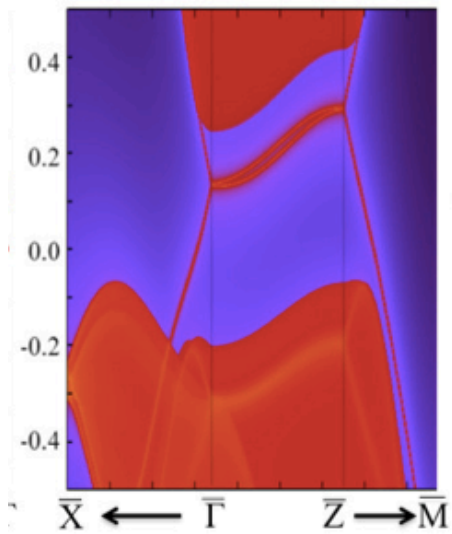
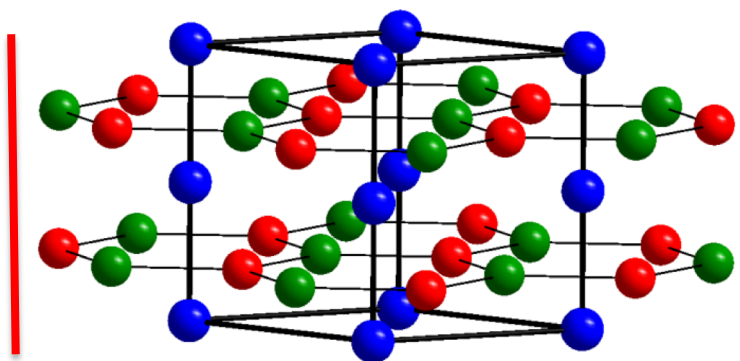


b)





# Honeycomb: Weak TI



KHgSb	KHgAs	KHgP
NaHgSb	NaHgAs	NaHgP
LiHgSb	LiHgAs	LiHgP
KCdSb	KCdAs	KCdP
NaCdSb	NaCdAs	NaCdP
LiCdSb	LiCdAs	LiCdP

KAuTe	KAuSe
NaAuTe	NaAuSe
LiAuTe	LiAuSe
KAgTe	KAgSe
NaAgTe	NaAgSe
LiAgTe	LiAgSe



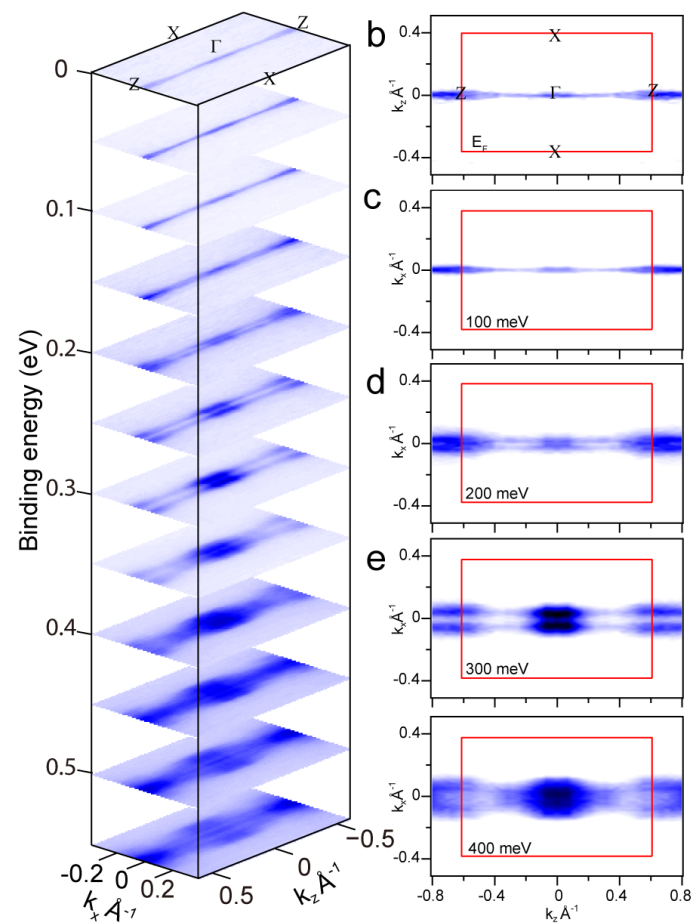
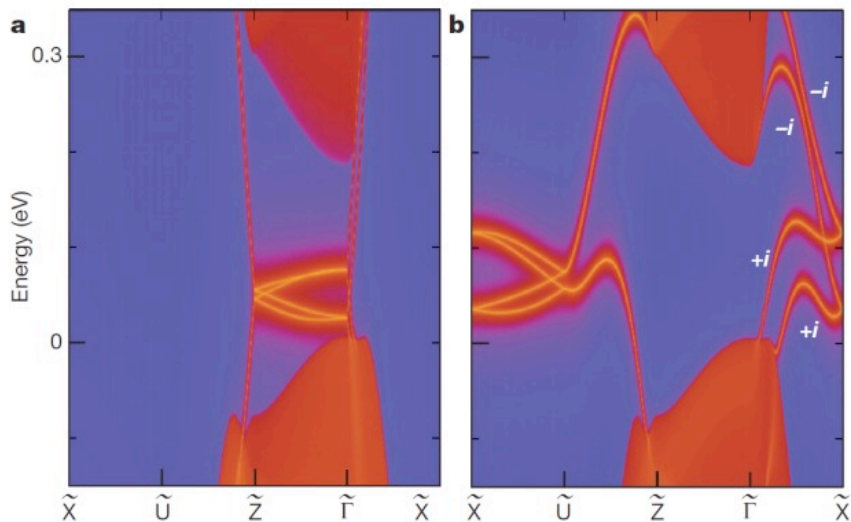
# Hourglass



## ARTICLE

# Hourglass fermions

Zhijun Wang<sup>1\*</sup>, A. Alexandradinata<sup>1,2\*</sup>, R. J. Cava<sup>3</sup> & B. Andrei Bernevig<sup>1</sup>



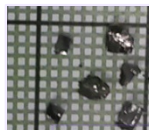
unpublished results



# Topology – interdisciplinary

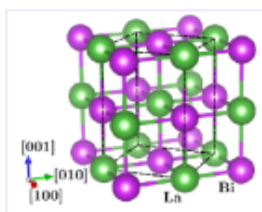
## Chemistry

Real space - local  
Crystals



LaBi

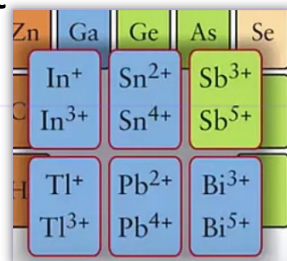
Crystal structure



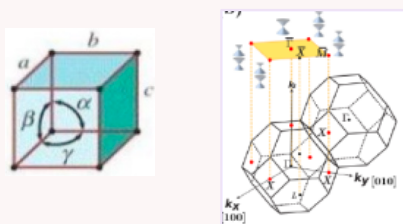
Position of the atoms

Check	WP	Representative
<input type="checkbox"/>	8g	x,y,z
<input type="checkbox"/>	4f	x,1/2,z
<input type="checkbox"/>	4e	x,0,z
<input checked="" type="checkbox"/>	4d	x,x,z
<input checked="" type="checkbox"/>	2c	1/2,0,z
<input type="checkbox"/>	1b	1/2,1/2,z
<input checked="" type="checkbox"/>	1a	0,0,z

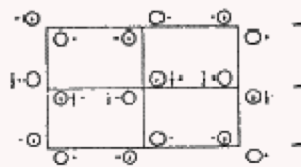
Inert pair effect



Symmetry



Local symmetry

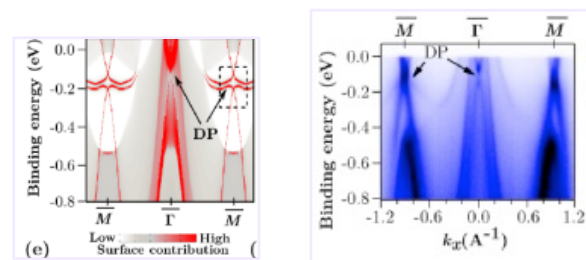


Relativistic effects

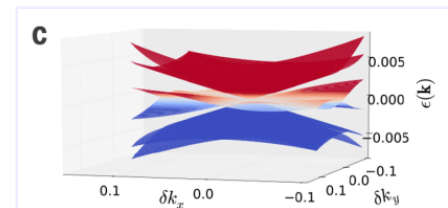
## Physics

Recipro. space - delocalized  
Brillouin zone

Electronic structure



Band connectivity



Dirac equation, Darwin term

$$H_{\text{Darwin}} = \frac{\hbar^2}{8m_e^2 c^2} (\Delta V)$$





# Topological Metals



# Rewriting the text book: Au



AUGUST 15, 1939

PHYSICAL REVIEW

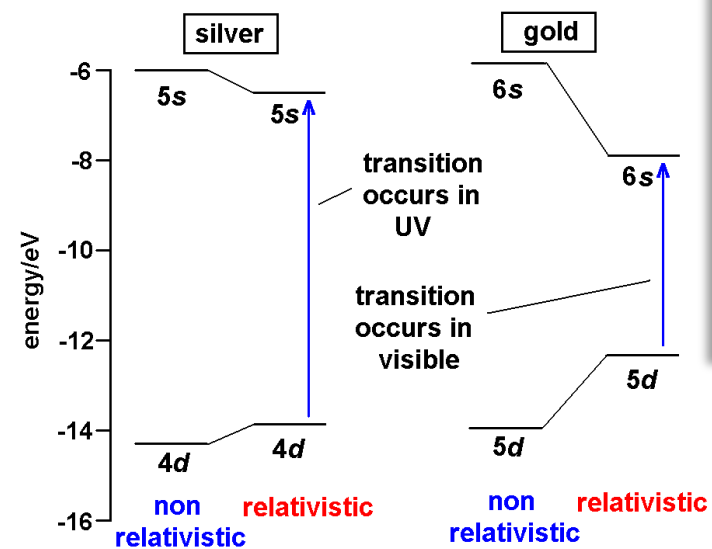
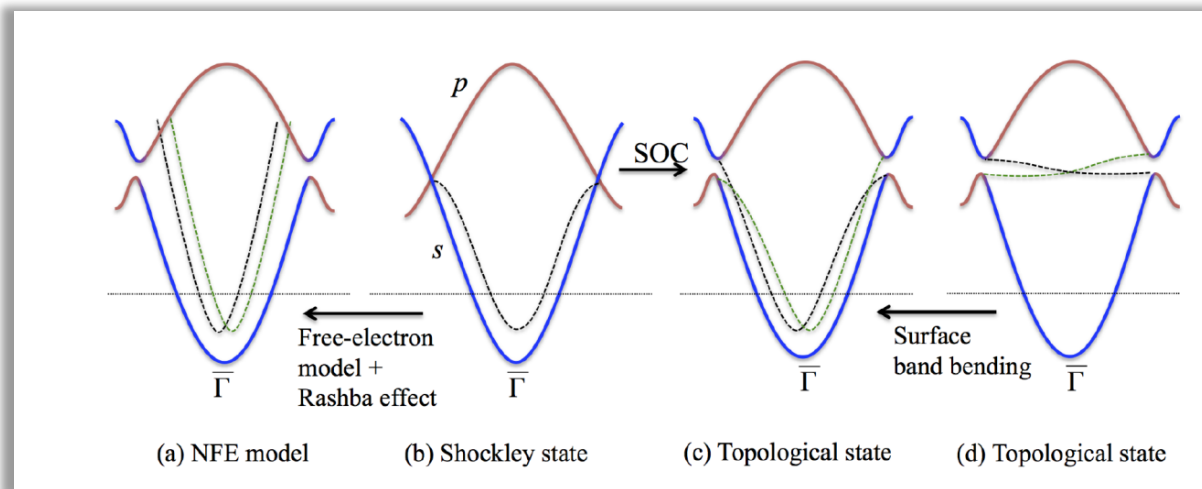
VOLUME 56

## On the Surface States Associated with a Periodic Potential

WILLIAM SHOCKLEY

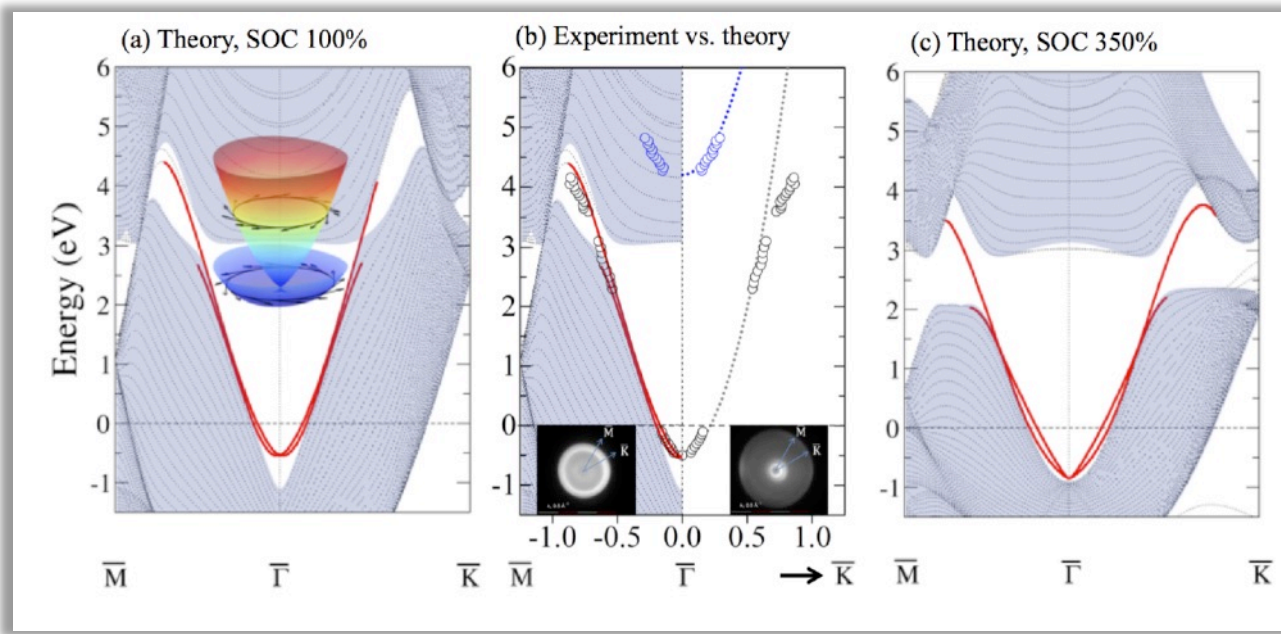
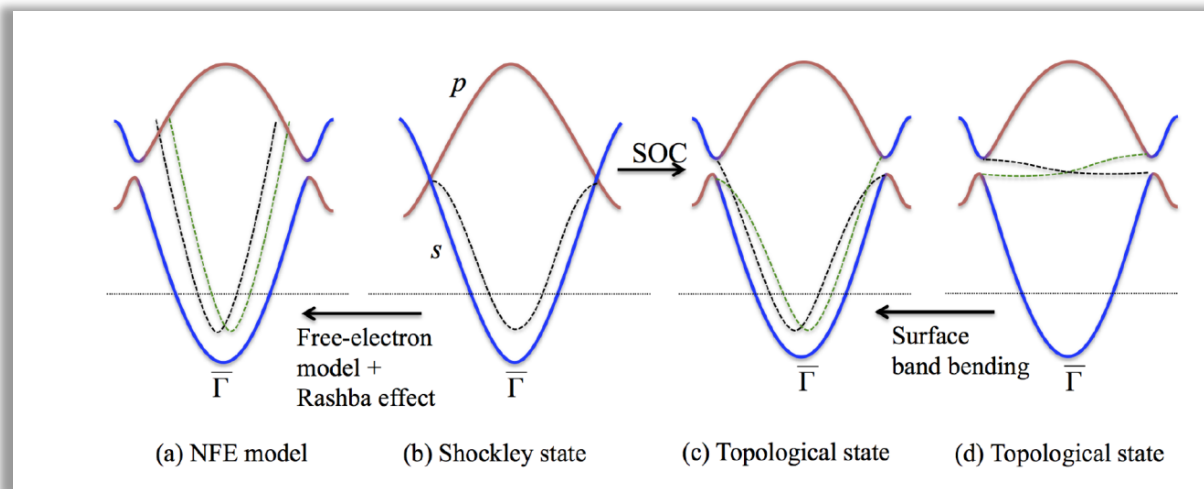
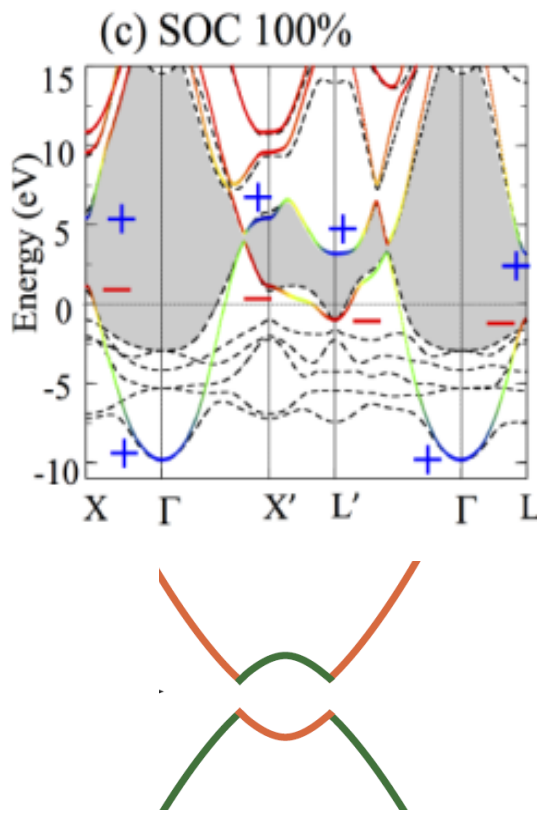
*Bell Telephone Laboratories, New York, New York*

(Received June 19, 1939)





# Rewriting the text book: Au



**Cs<sup>+</sup>Au<sup>-</sup>**



# New Fermions

RESEARCH

## RESEARCH ARTICLE SUMMARY

TOPOLOGICAL MATTER

# Beyond Dirac and Weyl fermions: Unconventional quasiparticles in conventional crystals

Barry Bradlyn,\* Jennifer Cano,\* Zhijun Wang,\* M. G. Vergniory, C. Felser, R. J. Cava, B. Andrei Bernevig†

Fermions in condensed-matter systems are not constrained by Poincare symmetry. Instead, they must only respect the crystal symmetry of one of the 230 space groups. Hence, there is the potential to find and classify free fermionic excitations in solid-state systems that have no high-energy counterparts.

What comes next? Magnetic Space groups

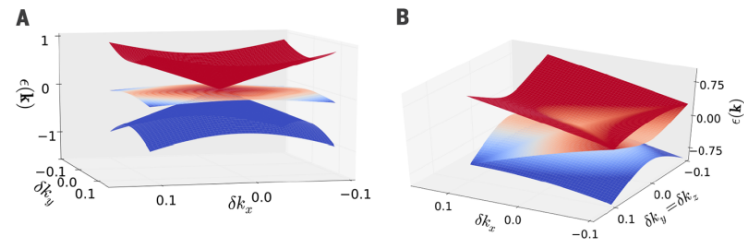
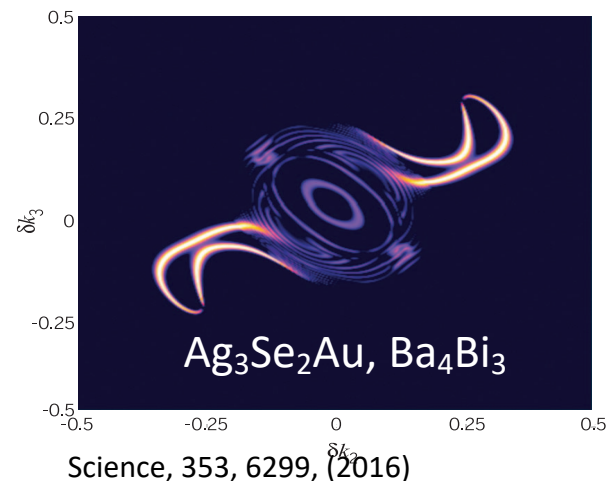
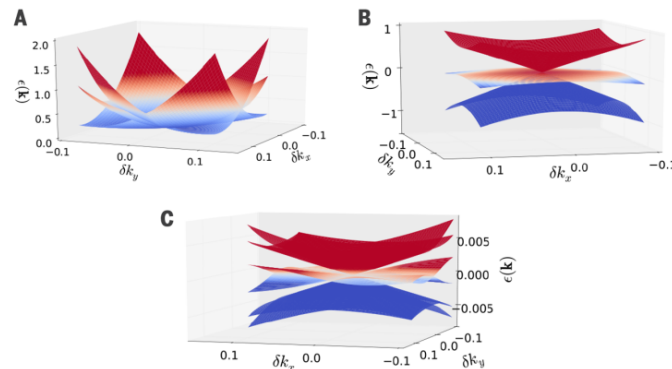


Fig. 1. Energy dispersion near a threefold degeneracy at the P point. (A and B) Shown are threefold degenerate points in (A) SGs 199 and 214 and (B) SG 220. In the latter case, pairs of bands remain degenerate in energy along the high-symmetry lines  $|\delta k_x| = |\delta k_y| = |\delta k_z|$ .





# Universe – applying a lattice



***Bringing  
order to the  
expanding  
fermion zoo***

Carlo Beenakker Commentary

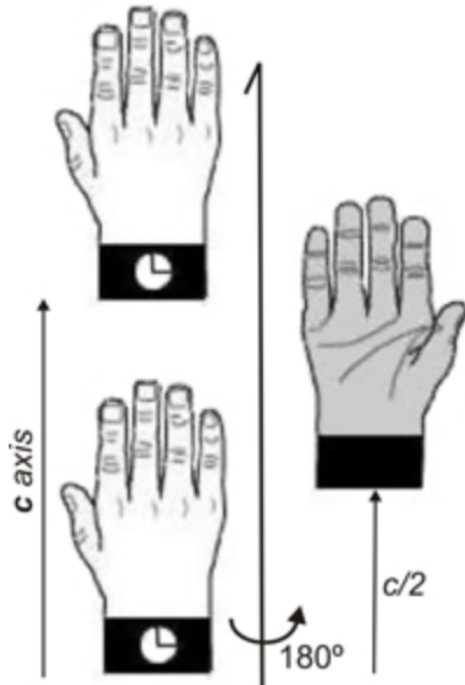
Heisenberg (1930): We observe space as a continuum, but we might entertain the thought that there is an underlying lattice and that space is actually a crystal. Which particles would inhabit such a lattice world? Werner Heisenberg *Gitterwelt* (lattice world) hosted electrons that could morph into protons, photons that were not massless, and more peculiarities that compelled him to abandon “this completely crazy idea”



# Non symmmorphic crystal structures

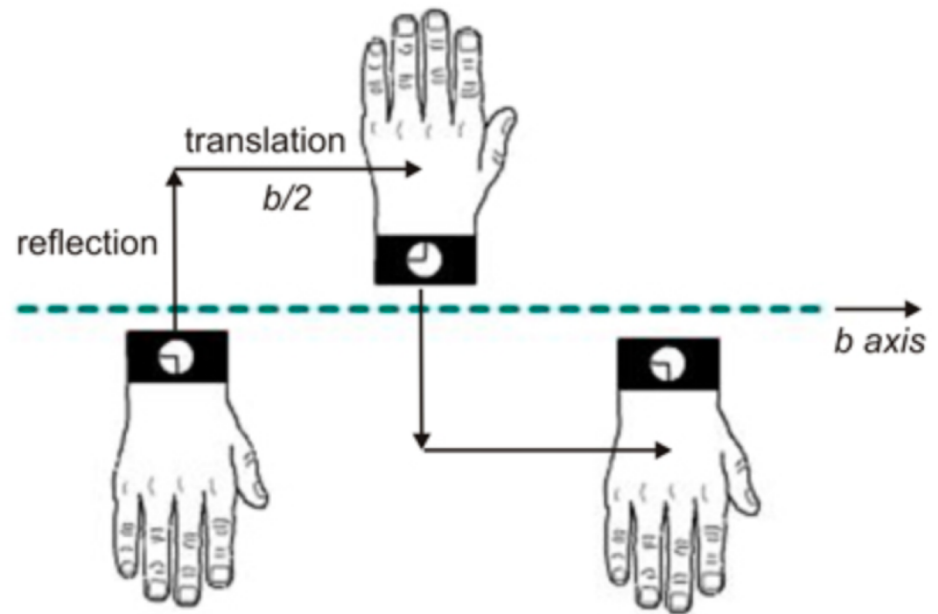


- non-symmorphic: elements with *fractional lattice translations*



*Twofold screw axis.*

*A screw axis consists of a rotation followed by a translation*



*Glide plane.*

*A glide plane consists of a reflection followed by a translation*



Exactly Match Elements

Cu & N



Search

1 H																	2 He
3 Li	4 Be										5 B	6 C	7 N	8 O	9 F	10 Ne	
11 Na	12 Mg										13 Al	14 Si	15 P	16 S	17 Cl	18 Ar	
19 K	20 Ca	21 Sc	22 Ti	23 V	24 Cr	25 Mn	26 Fe	27 Co	28 Ni	29 Cu	30 Zn	31 Ga	32 Ge	33 As	34 Se	35 Br	36 Kr
37 Rb	38 Sr	39 Y	40 Zr	41 Nb	42 Mo	43 Tc	44 Ru	45 Rh	46 Pd	47 Ag	48 Cd	49 In	50 Sn	51 Sb	52 Te	53 I	54 Xe
55 Cs	56 Ba	57-71 La-Lu	72 Hf	73 Ta	74 W	75 Re	76 Os	77 Ir	78 Pt	79 Au	80 Hg	81 Tl	82 Pb	83 Bi	84 Po	85 At	86 Rn
87 Fr	88 Ra	89-103 Ac-Lr	104 Rf	105 Db	106 Sg	107 Bh	108 Hs	109 Mt	110 Ds	111 Rg	112 Cn						

57 La	58 Ce	59 Pr	60 Nd	61 Pm	62 Sm	63 Eu	64 Gd	65 Tb	66 Dy	67 Ho	68 Er	69 Tm	70 Yb	71 Lu
89 Ac	90 Th	91 Pa	92 U	93 Np	94 Pu	95 Am	96 Cm	97 Bk	98 Cf	99 Es	100 Fm	101 Md	102 No	103 Lr



Found 4 entries, showing 4

ID	↑↓ Formula ↑↓	Space Group	↑↓ NSOC Topo Class	↑↓ SOC Topo Class	↑↓ NSOC Gap	↑↓ SOC Gap	↑↓ Action
MAT00013130	FeSi <sub>2</sub>	64	Triv_Ins	Triv_Ins	N/A	N/A	<a href="#">View Details</a>
MAT00015330	FeSi <sub>2</sub>	123	HSL_SM	TCI	0	0	<a href="#">View Details</a>
MAT00022653	Fe <sub>5</sub> Si <sub>3</sub>	193	HSP_SM	HSL_SM	0	0	<a href="#">View Details</a>
MAT00023895	FeSi	198	Triv_Ins	Triv_Ins	N/A	N/A	<a href="#">View Details</a>